Statistical physics for non-physics problems

Application of paradigms of equilibrium statistical physics to social sciences: from obesity epidemic to diffusion of innovation in society

Collaborators



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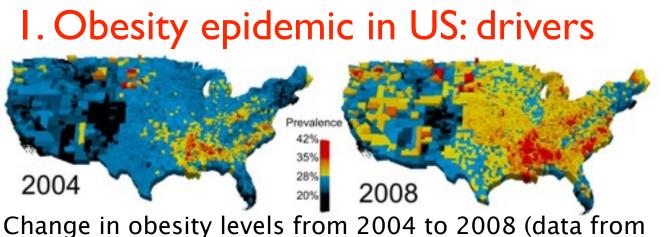


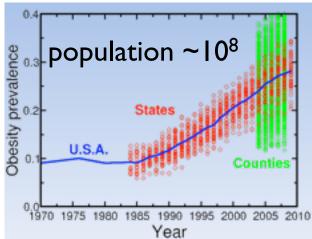
H. Eugene Stanley Boston University Physics



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Funding: NSF, ARL, EC

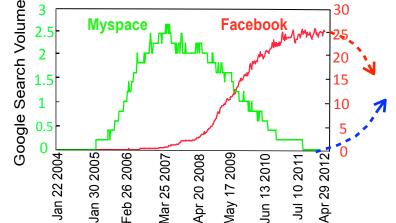




2. Theory that predicts the tipping point of disintegration

myspace vs facebook Can we predict the next facebook? Predict the minimum number of pioneers that, upon leaving, will fragment the network

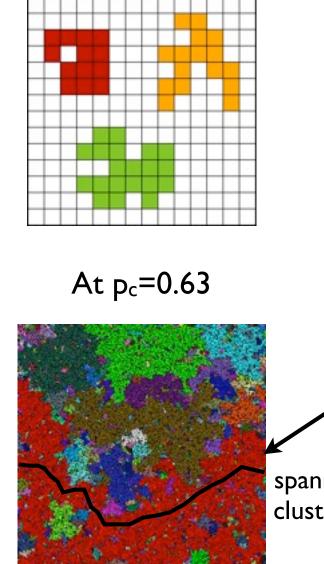
facebook ~ 10^9 users **Facebook Myspace**

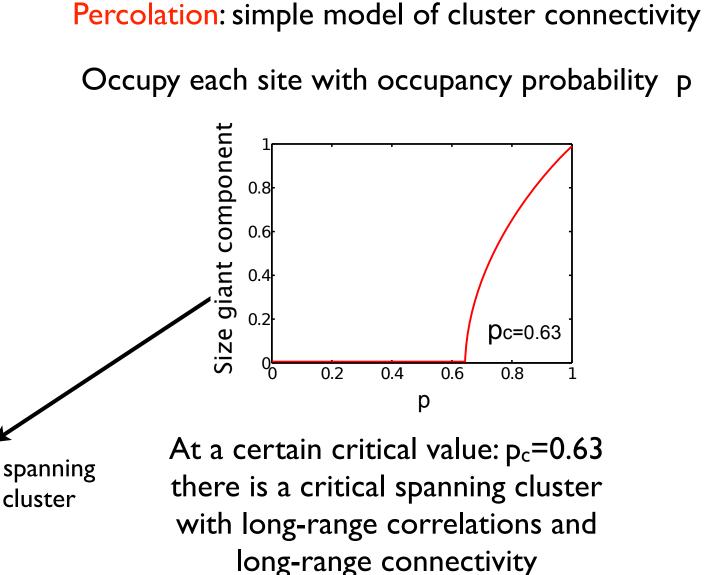


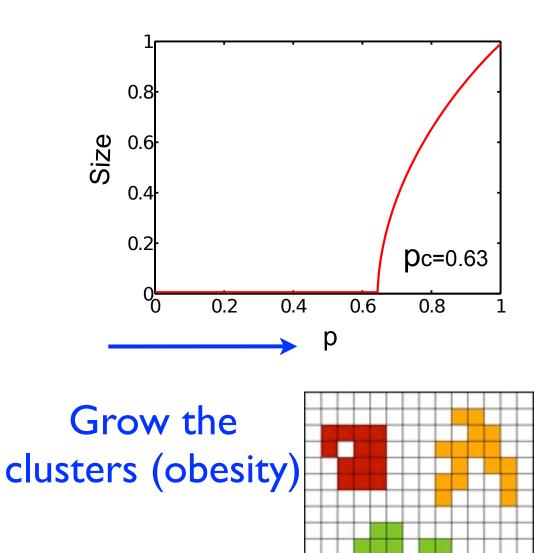
Tools: Percolation theory and collective behavior in critical phase transitions

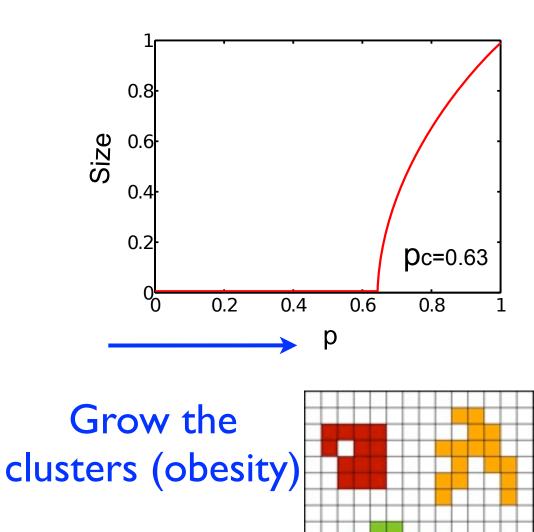
Common physical model: Percolation theory

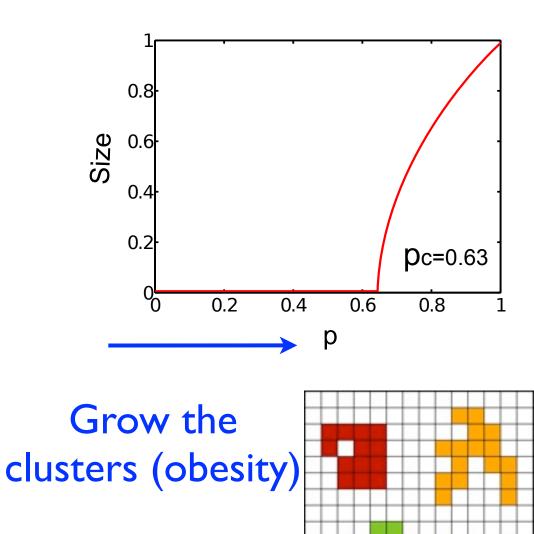
Low p<pc=0.63

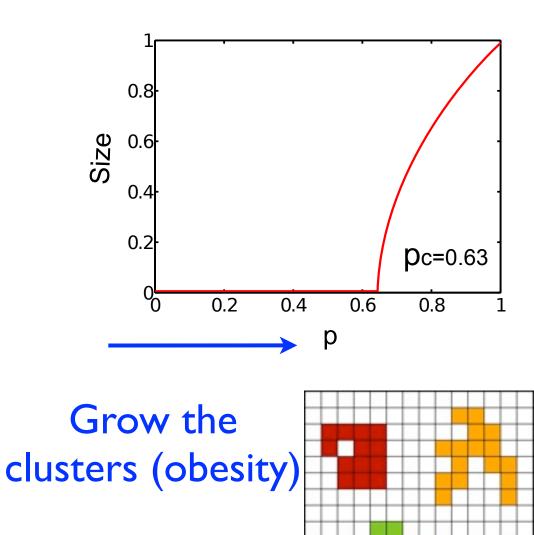


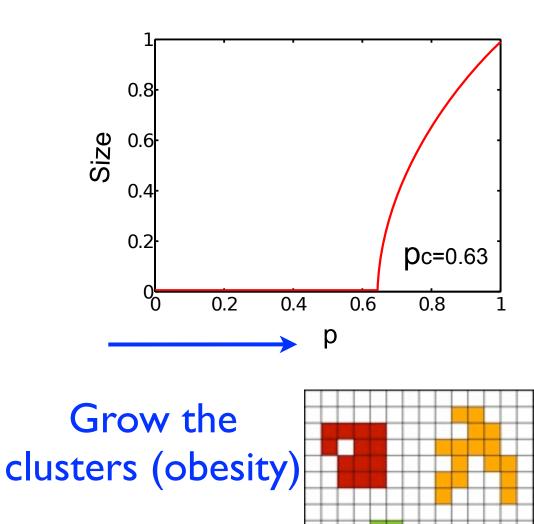


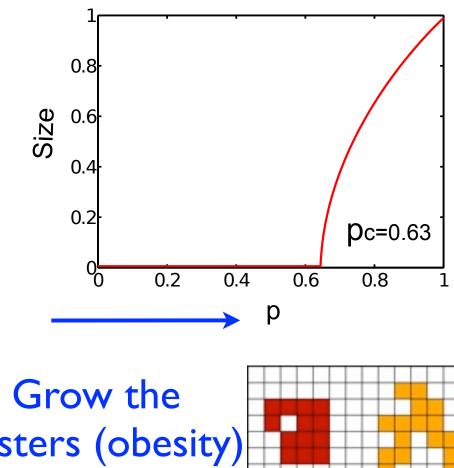




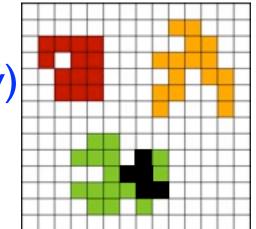


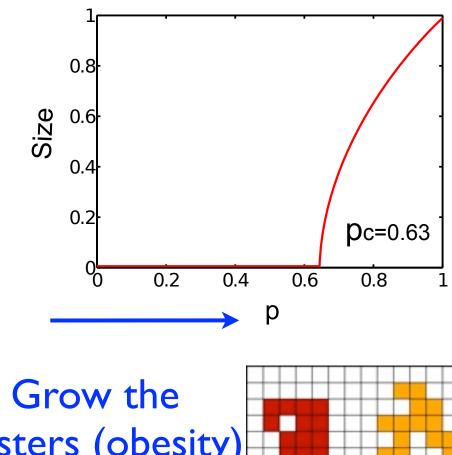




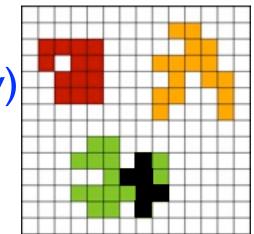


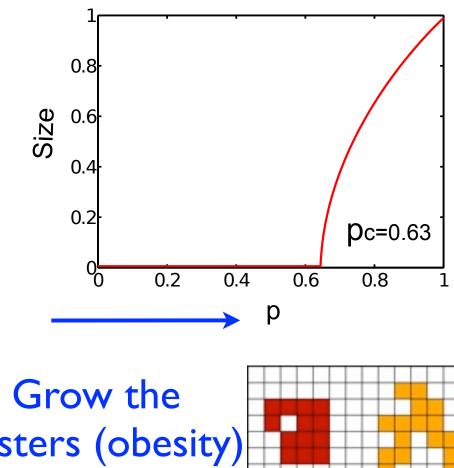
clusters (obesity)



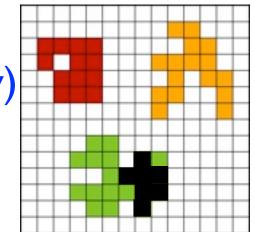


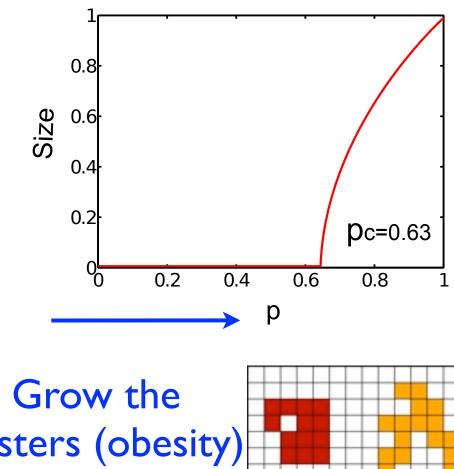
Grow the clusters (obesity)



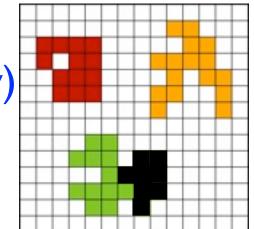


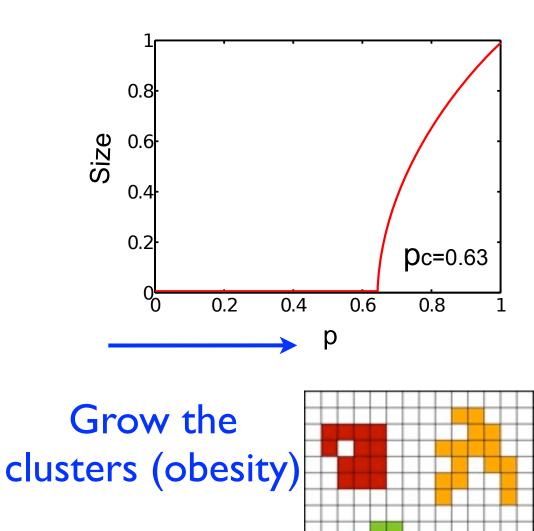
clusters (obesity)

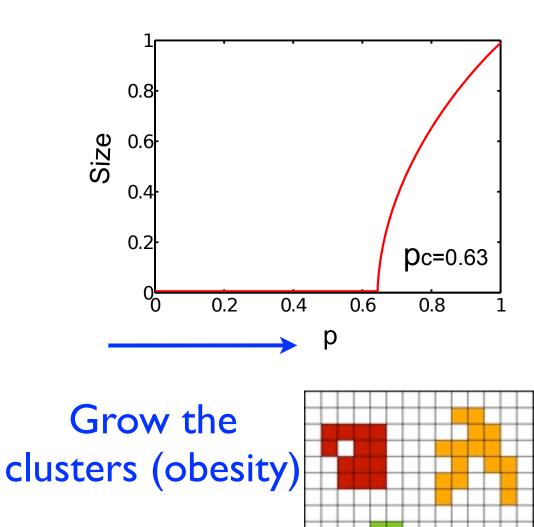


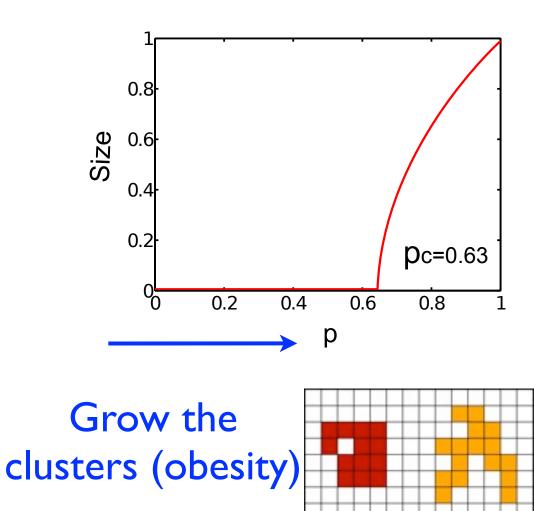


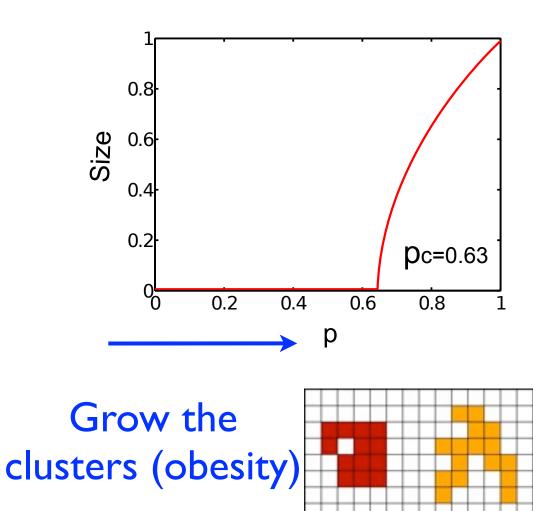
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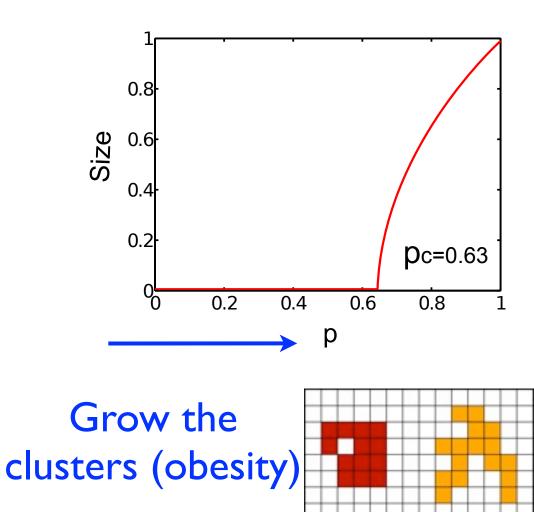


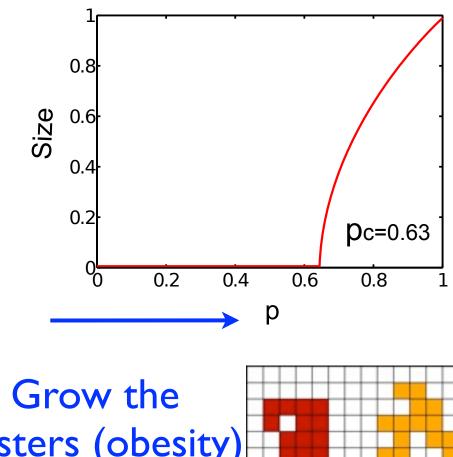




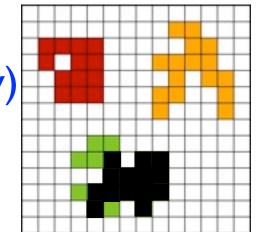


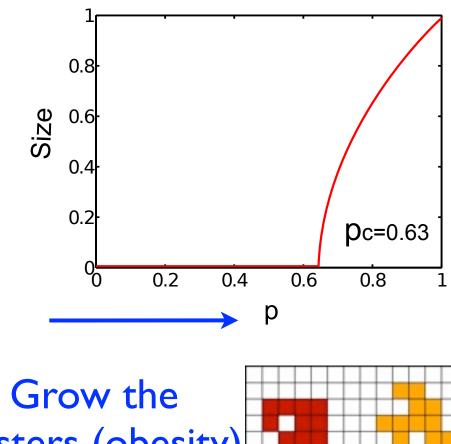




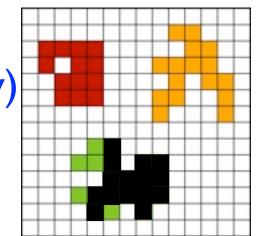


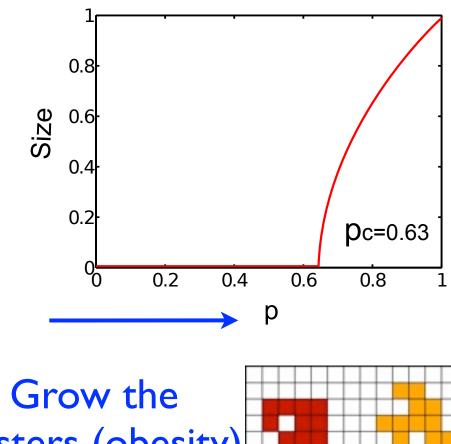
clusters (obesity)



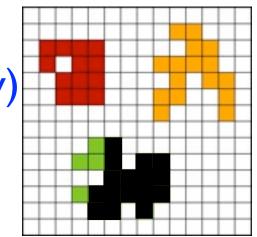


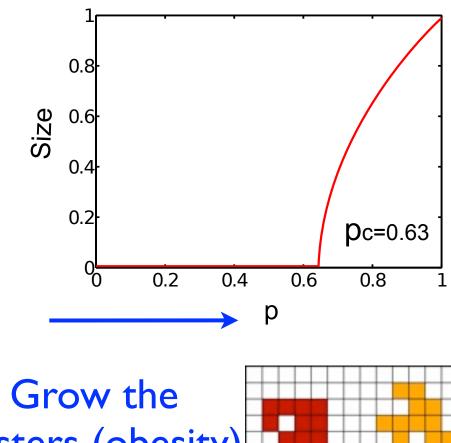
Grow the clusters (obesity)



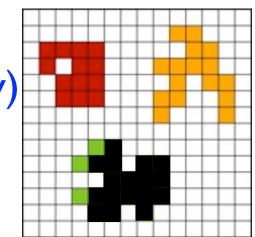


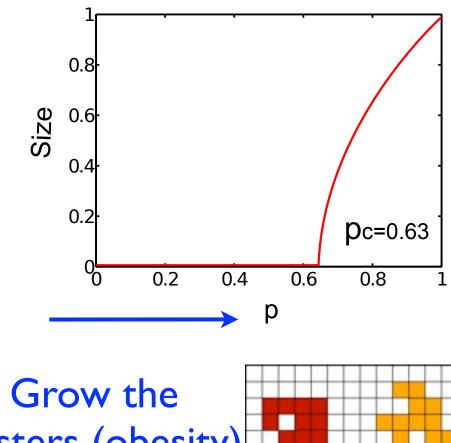
Grow the clusters (obesity)



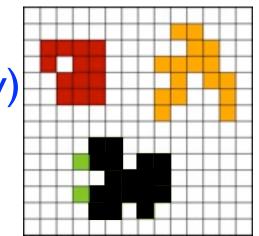


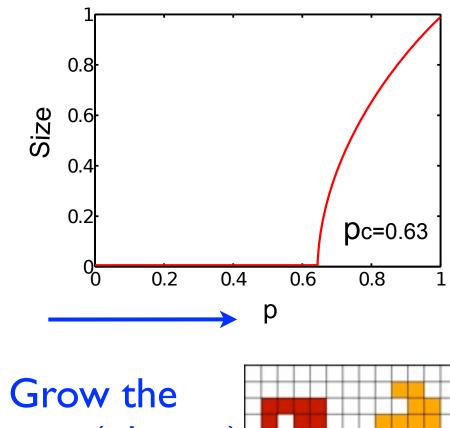
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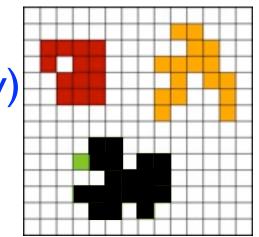


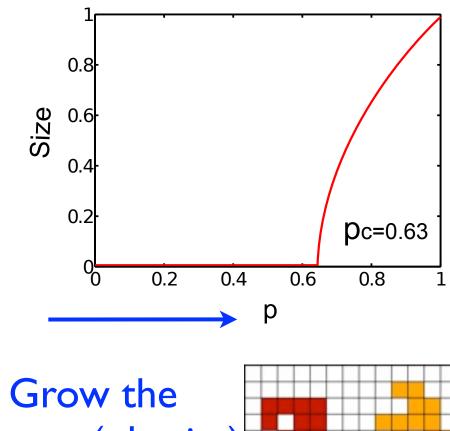
Grow the clusters (obesity)



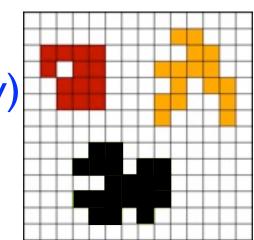


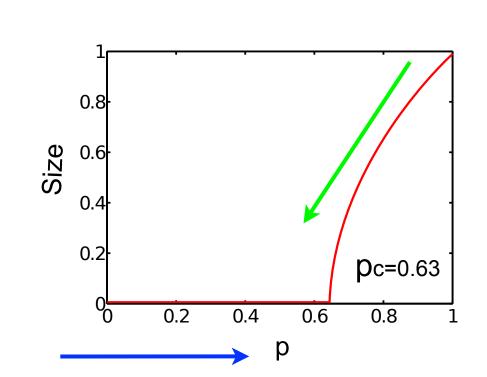
clusters (obesity)



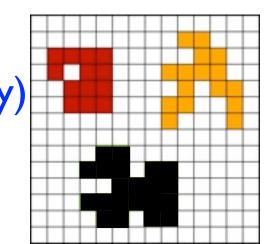


Grow the clusters (obesity)

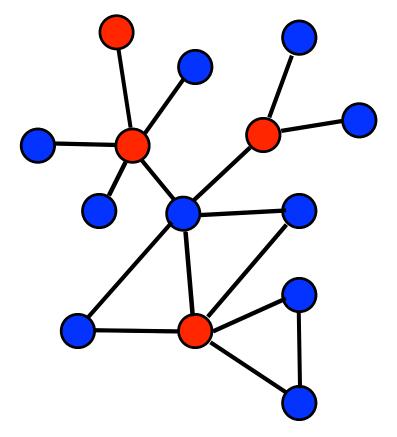




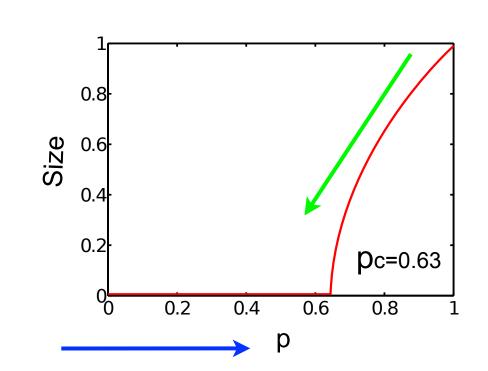
Grow the clusters (obesity)



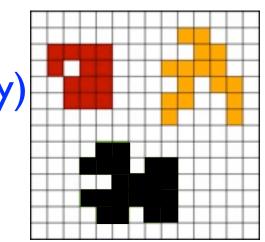
"Attack" a network: Fragmentation of social networks



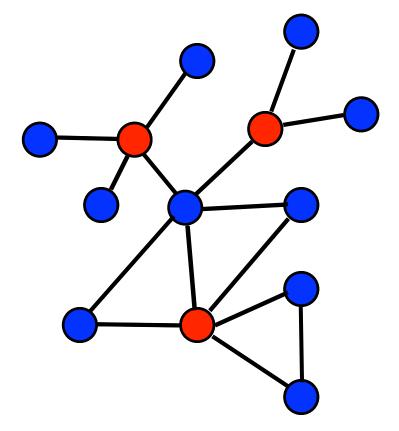
1-p: minimum number of nodes to disrupt the network



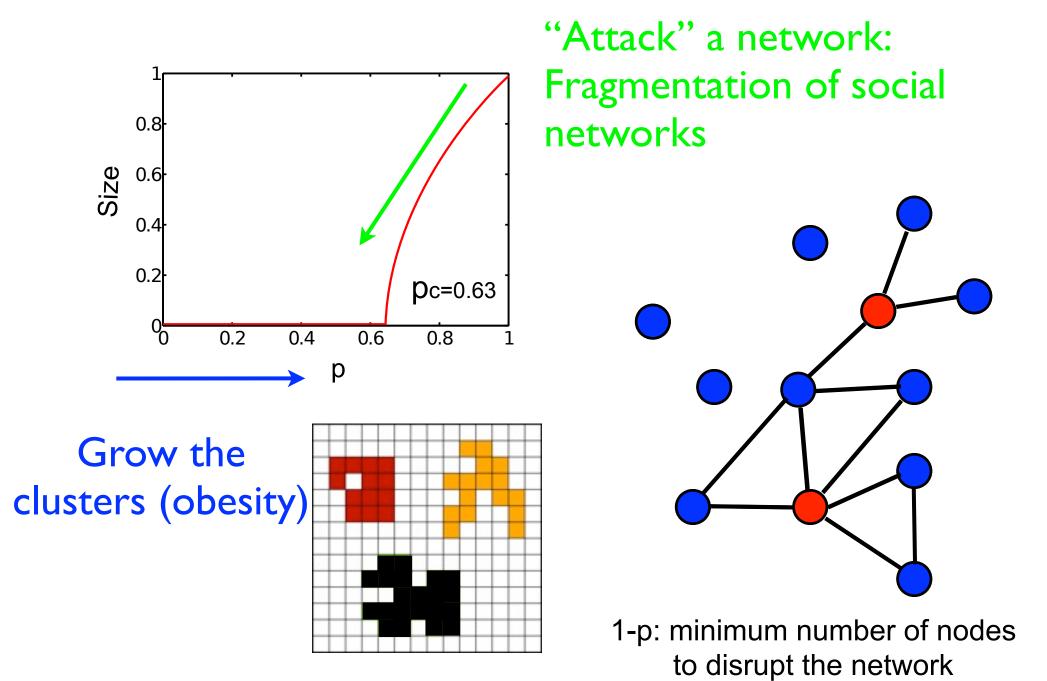
Grow the clusters (obesity)

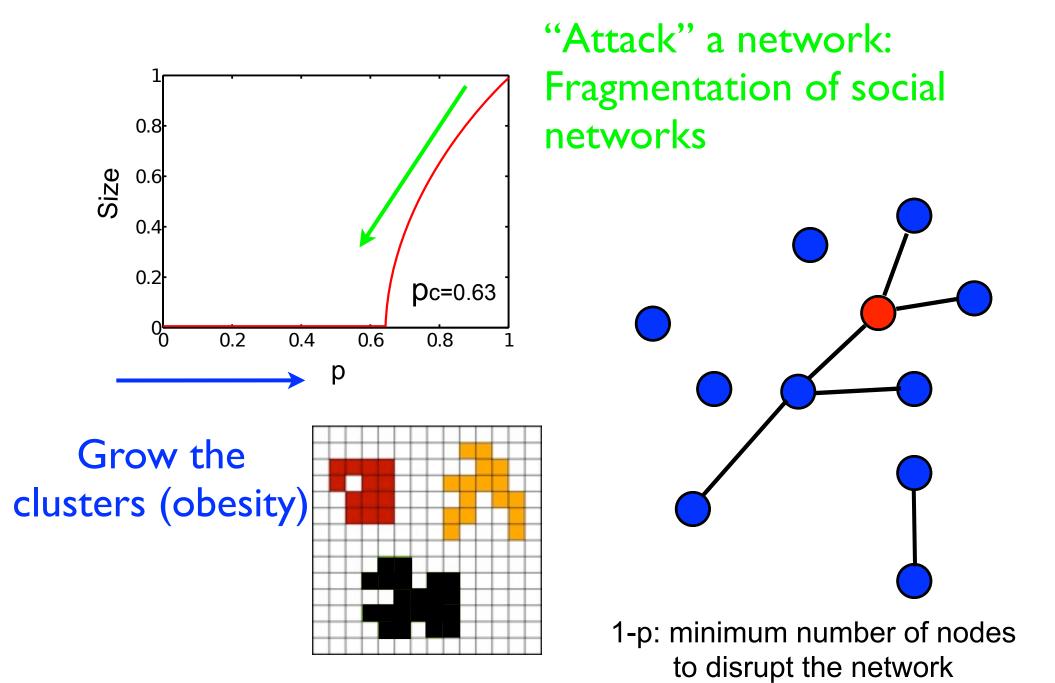


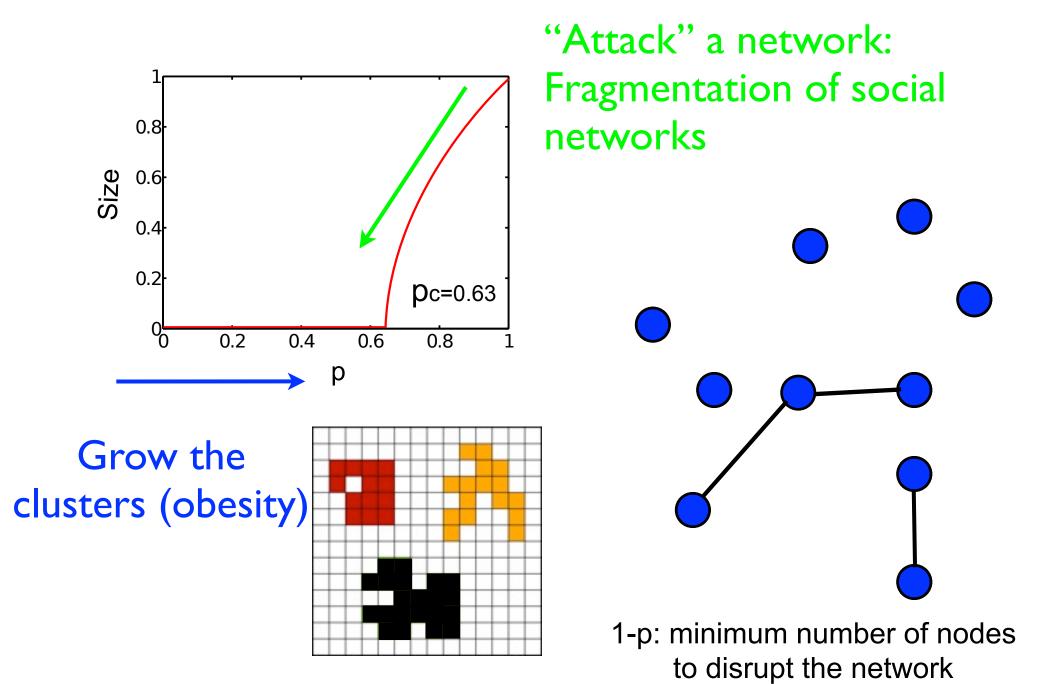
"Attack" a network: Fragmentation of social networks



1-p: minimum number of nodes to disrupt the network







Obesity percolation: hierarchical clustering

red bond: Rich, UT

Using CDC data at county level to investigate the spatial spreading of obesity

red bond: Mc Lean, KY

2004

Obese: BMI>30

epicenter: Greene county, AL

Obesity percolation: hierarchical clustering

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Obesity percolation: hierarchical clustering

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Using CDC data at county level to investigate the spatial spreading of obesity

red bond: Mc Lean, KY

2004

Obese: BMI>30

epicenter: Greene county, AL

What is driving the global obesity epidemic?

Hotly debated question: relevant for implementing health policies

Experts say:

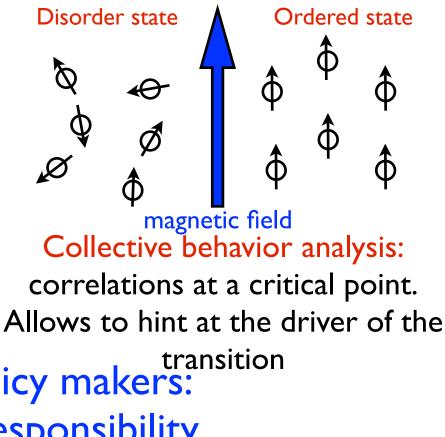
A. Individuals responsibility:

Genetic make-up Individual habits: poor diet Peer pressure via social network (Christakis, JAMA, 2007)

B. Environmental global effect

(The Lancet, 2011): Obesity is driven by global food marketing system: a predictable outcome of market economies predicated on consumptionbased growth. Physics says:

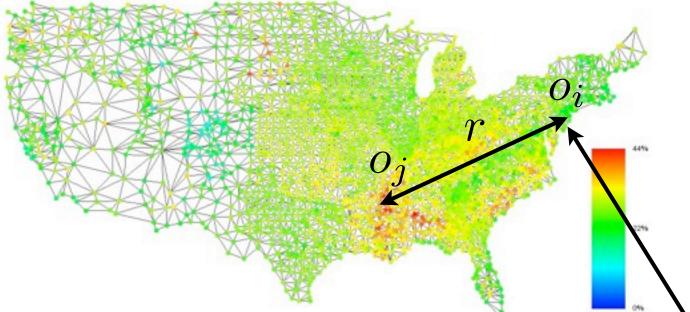
Spin up = obese Spin down = not obese



Important issue for policy makers: Individual vs Industry responsibility

Searching for correlations

Drivers of the epidemic: collective behavior or individual habits



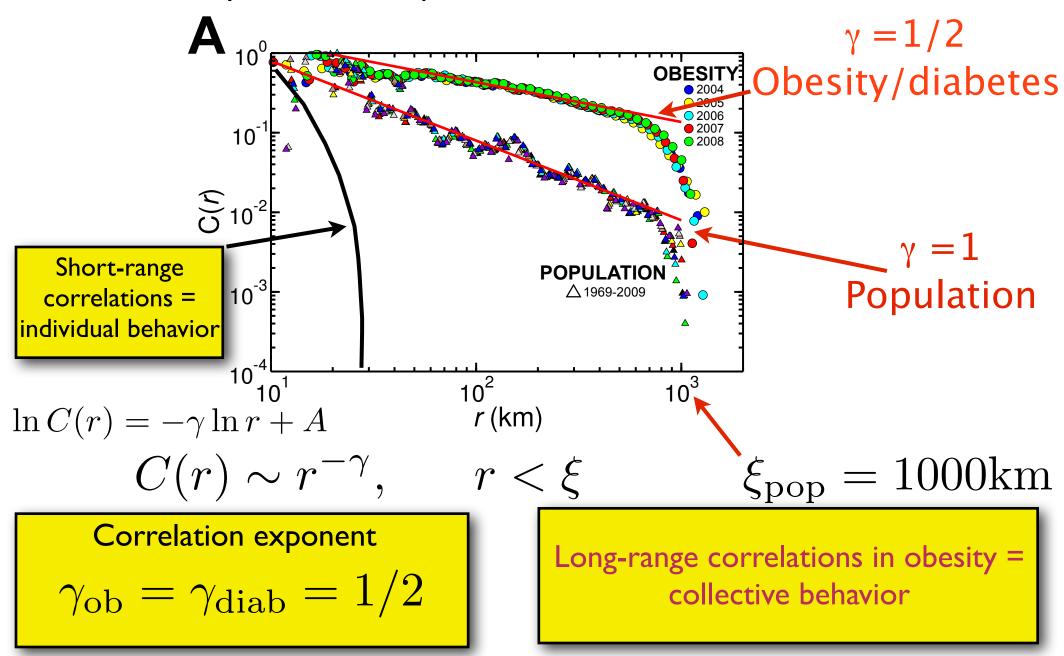
Correlation function of the obesity prevalence, o_i, defined at the county level. Data from CDC

How obesity prevalence at position i influences the obesity at a distance r

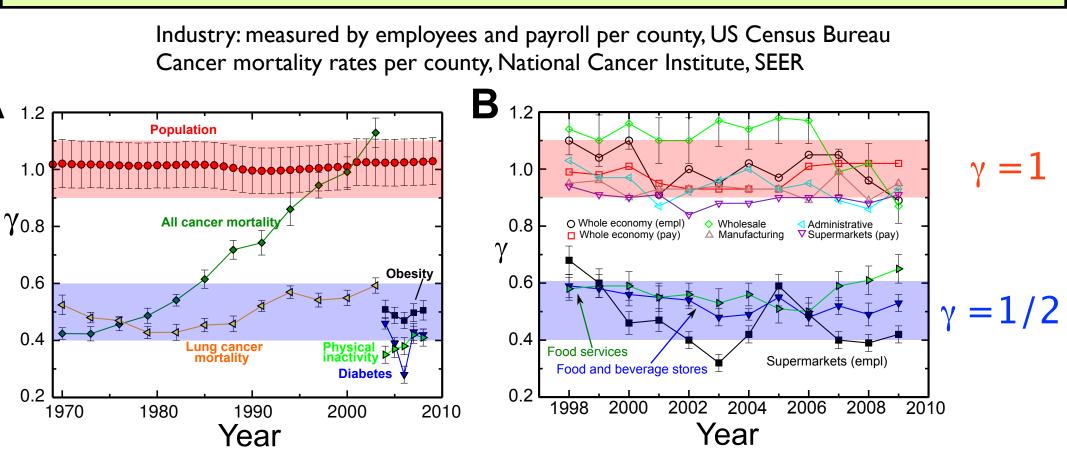
$$C(r) = \frac{1}{\sigma^2} \sum_{ij} \left(o_i - \bar{o} \right) \left(o_j - \bar{o} \right)$$

Obesity is long-ranged correlated up to 1000km





What about the food industry's activity?



Obesity fluctuations are synchronized with supermarket fluctuations

Conjecture:

Driving force of obesity: economic activity of food industry?

It may not be all about calories

- Obesity spreading is analogous to strongly correlated physical systems
- We live in 'obesity cities' which are much larger than real cities (~ 1000 km)
- The obesity problem is the same all across USA, including the lower prevalence areas (NY, West coast)
- Population distribution has much weaker correlations
- Strong correlations in food industry too (driver?)

Should policies target mainly the global food system, rather than individual behaviors?

Michelle Obama's "Let's move" campaign vs NYC Major Bloomberg's super-sized soda ban

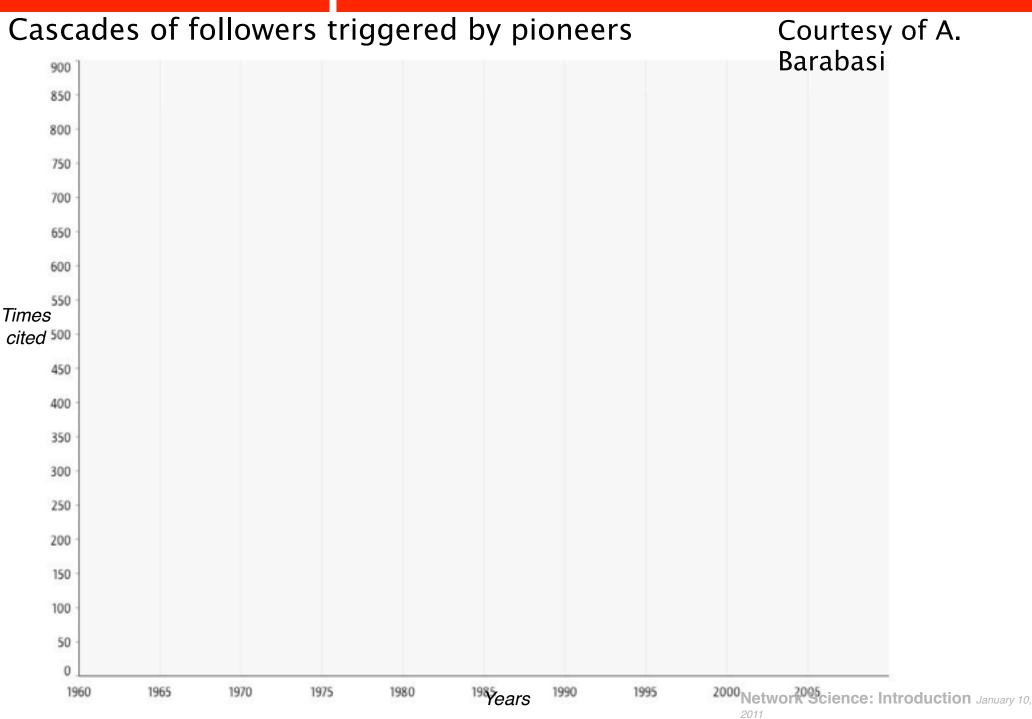
NETWORK SCIENCE The rise of scientific ideas

Cascades of followers triggered by pioneers

Courtesy of A. Barabasi

Times cited

NETWORK SCIENCE The rise of scientific ideas

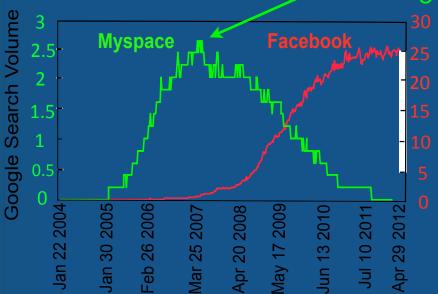


Rise and fall of social networks: how novel ideas are adopted in a social community

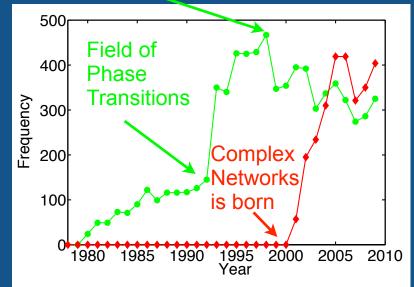
Myspace vs Facebook

Scientific communities:

"Phase Transition" vs "Networks science"



Predicting the tipping point ~



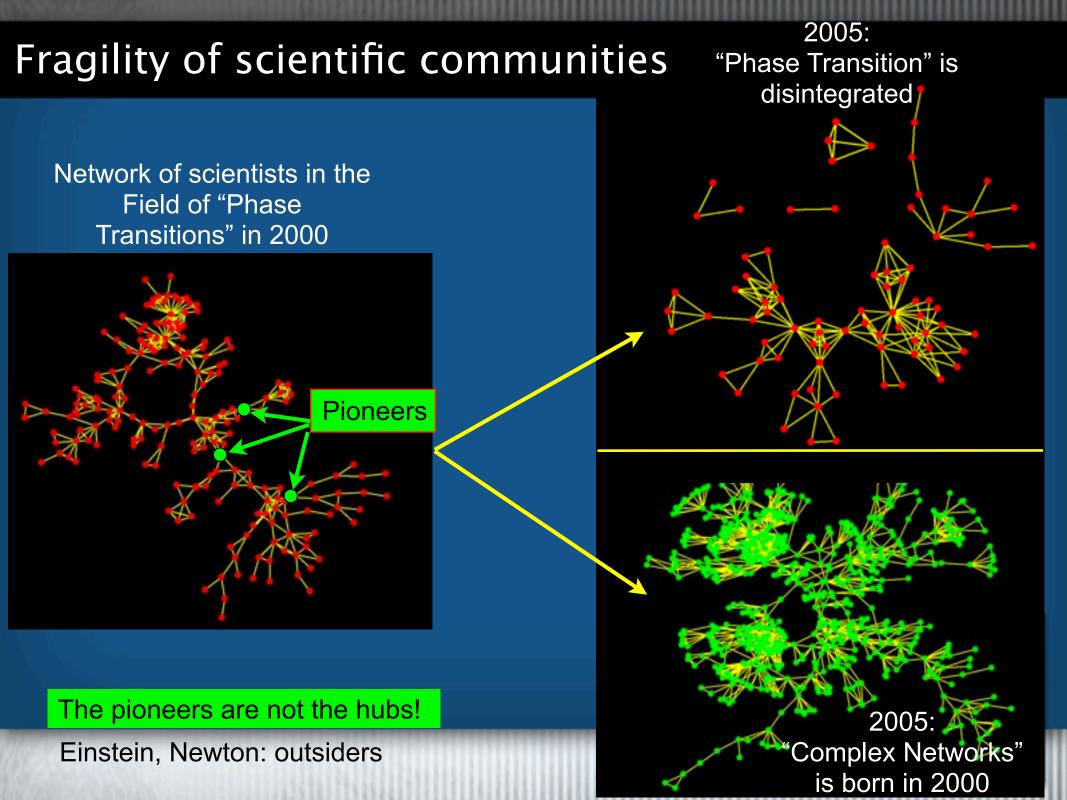
Collaboration of scientists publishing in the American Physical Society (APS)

Other applications:

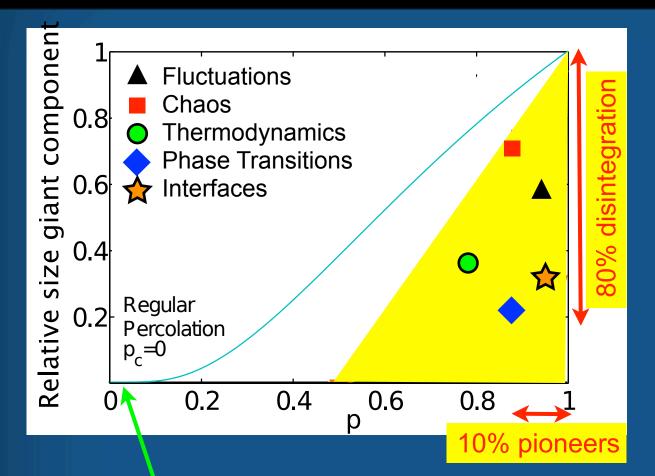
Disintegration of political systems: "Arab spring" Adoption of consumer products, art and scientific trends Marketing of brand new products Market crash

How to identify the conditions for fragmentation?





Fragility of scientific communities



Social networks are scalefree, yet they are extremely fragile to the departure of a few pioneers, who are not hubs.

We find:

 $p_c \in [0.5, 0.9]$

Data contrasts with prediction of percolation theory on scale-free networks:

 $p_c = \frac{\langle k \rangle}{\langle k^2 \rangle}$

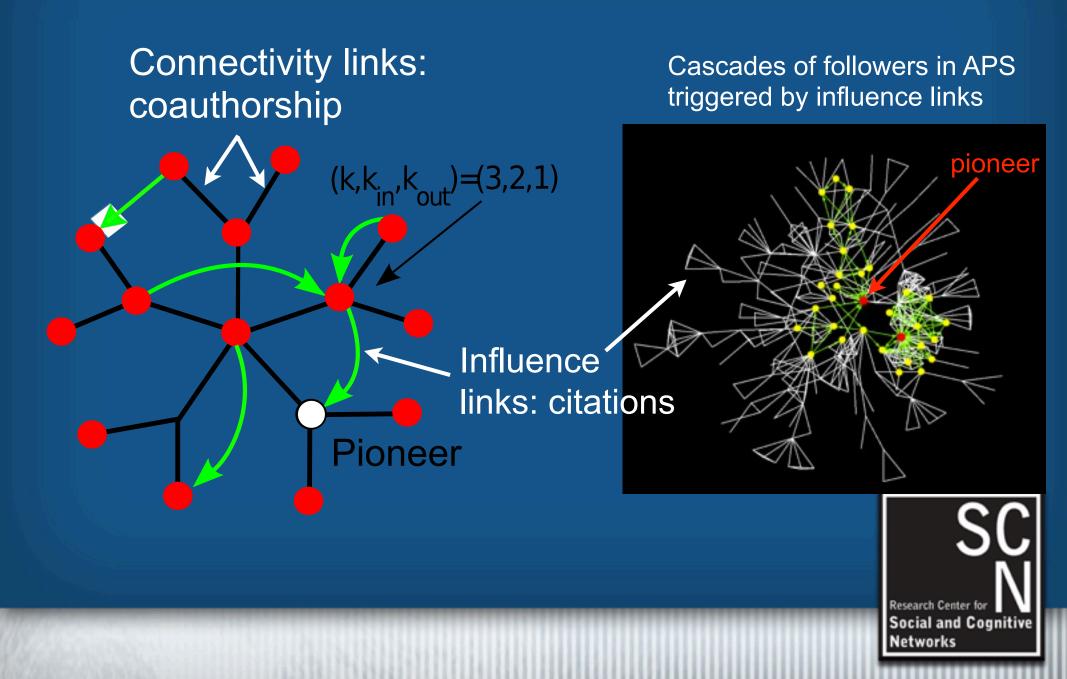
$$P(k) \sim k$$

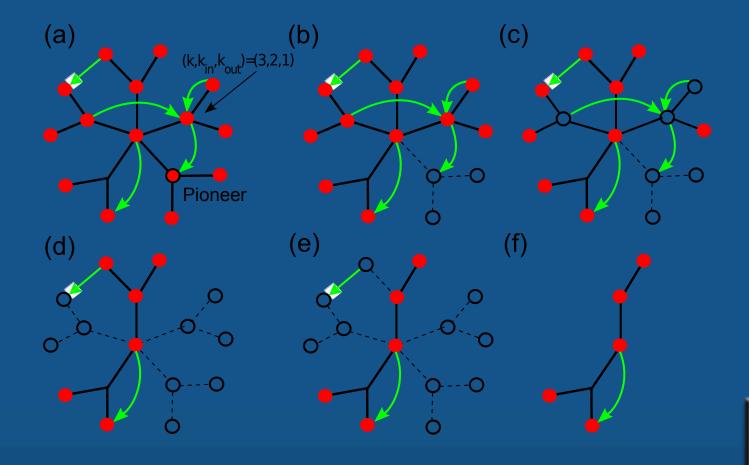
 $p_c = 0$

Scale-free networks: Robust to random attack, yet fragile to hub attack.

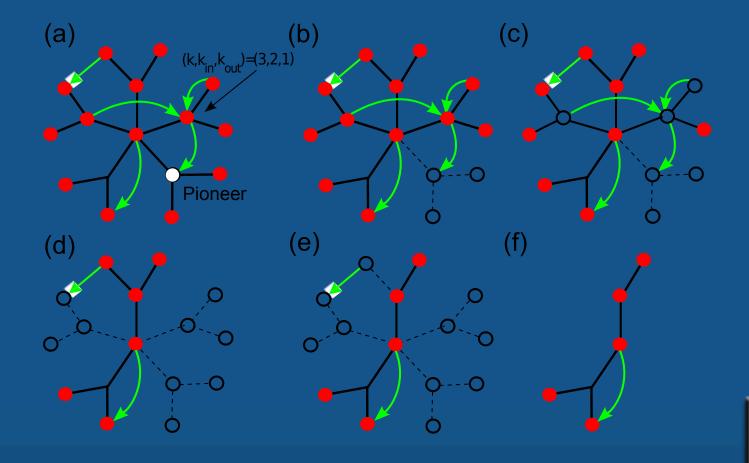


Two networks: connectivity + influence

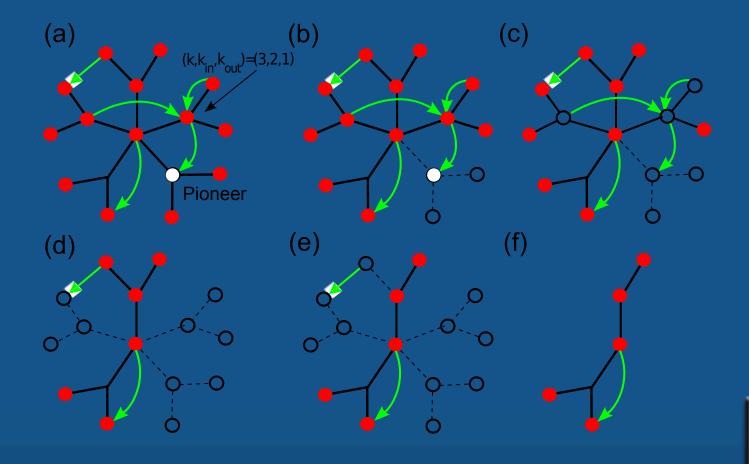




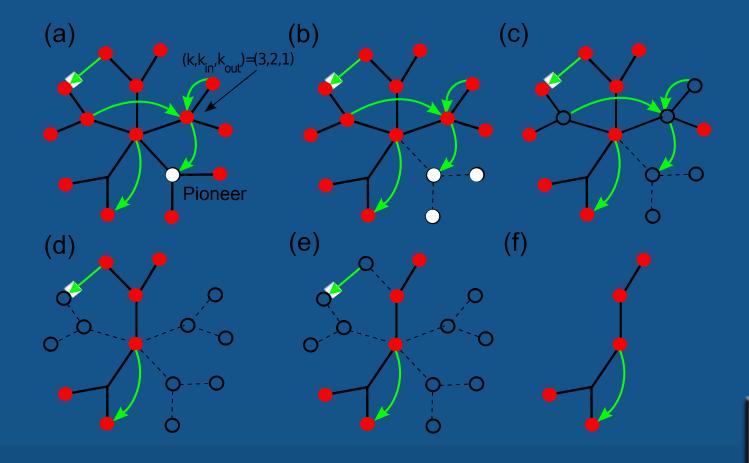




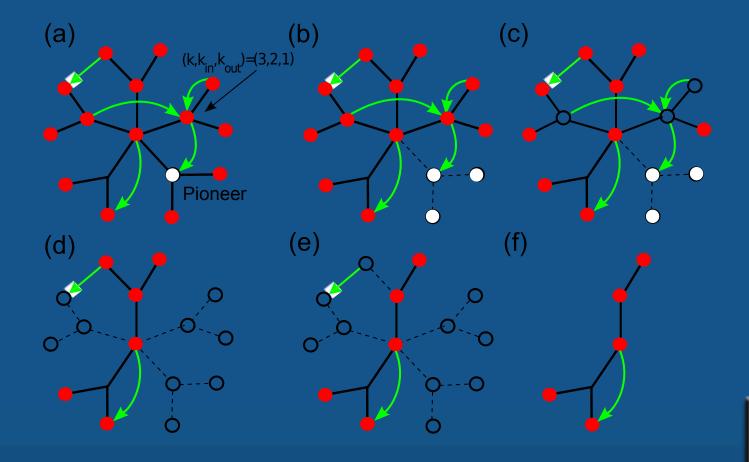




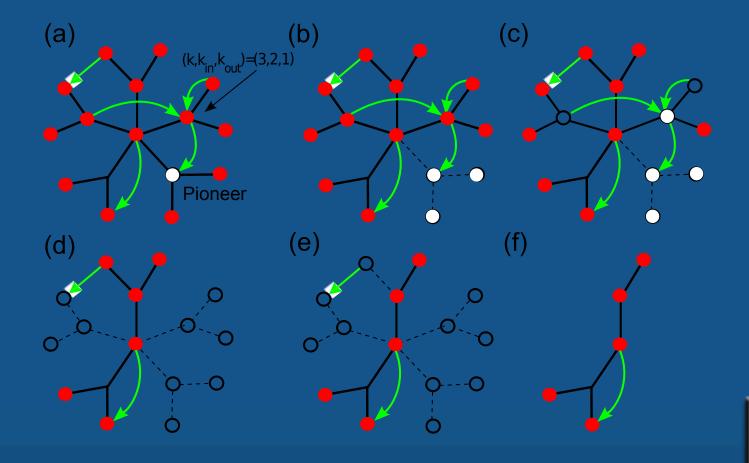




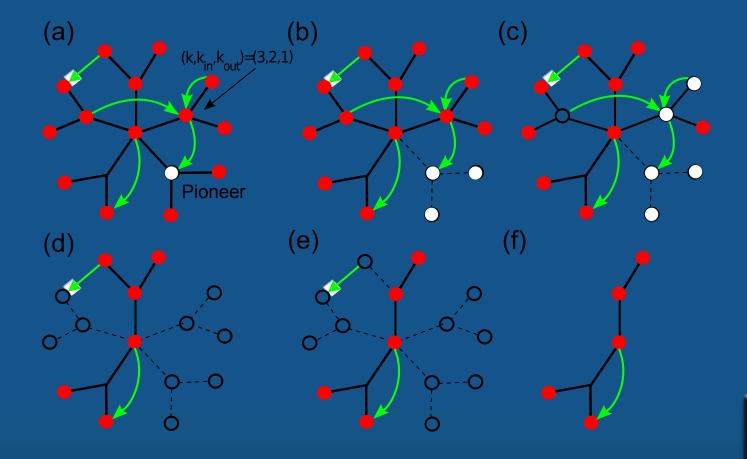




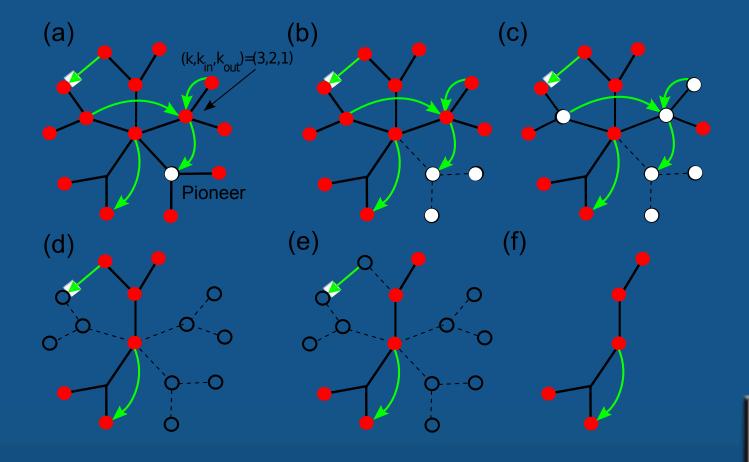




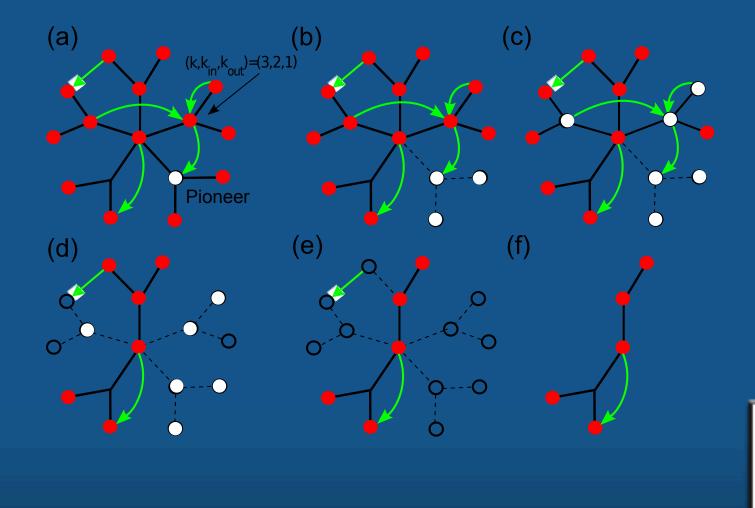




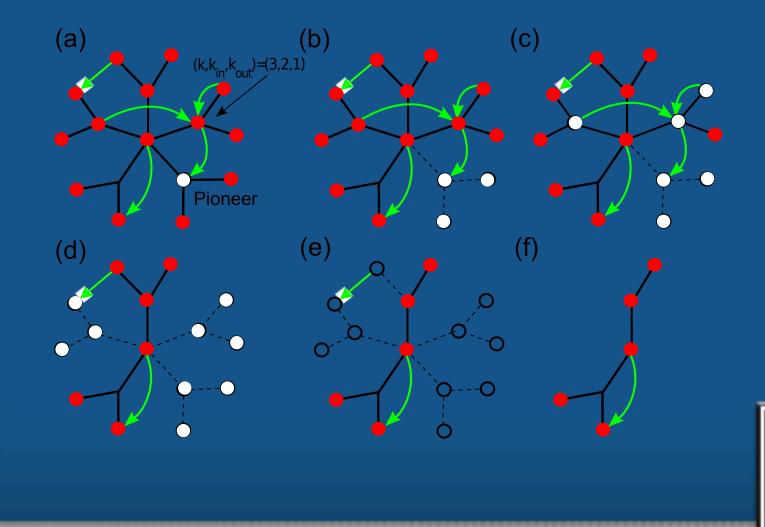




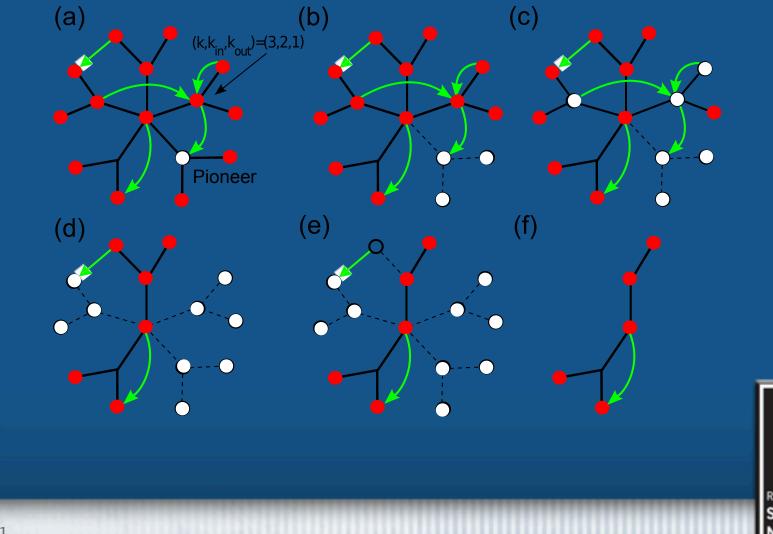




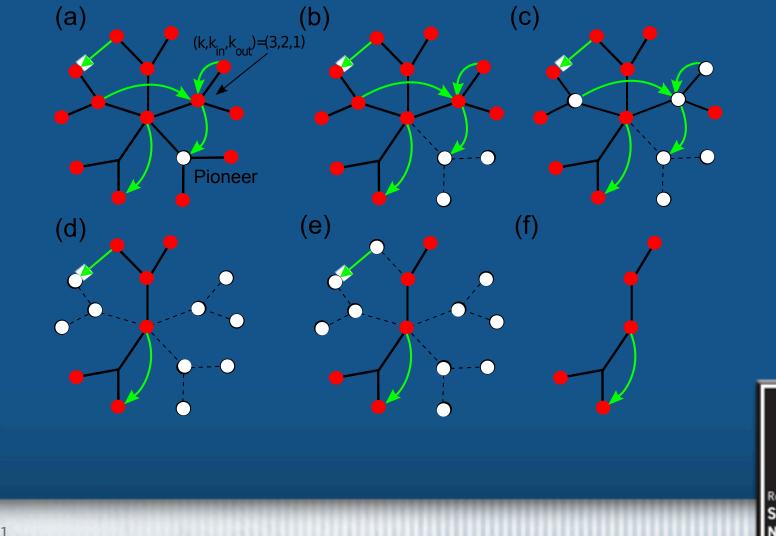






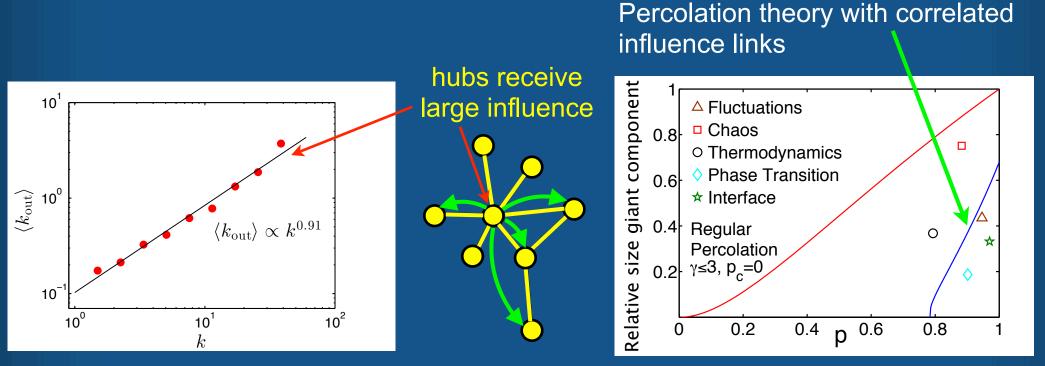








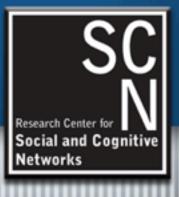
Theoretical prediction of the tipping point Why networks are so fragile?



We predict the conditions at the tipping point:

- 1. Hubs are not pioneers
- 2. Pioneers are small players who initiate cascade of followers
- 3. Hubs jump into the "new idea" and sustain the cascade
- 4. Fragmentation: strong correlation between hubs connectivity and out-degree of influence

Conclusion: two conditions for fragmentation: (1) Existence of hubs. (2) Hubs are aware of latest trends

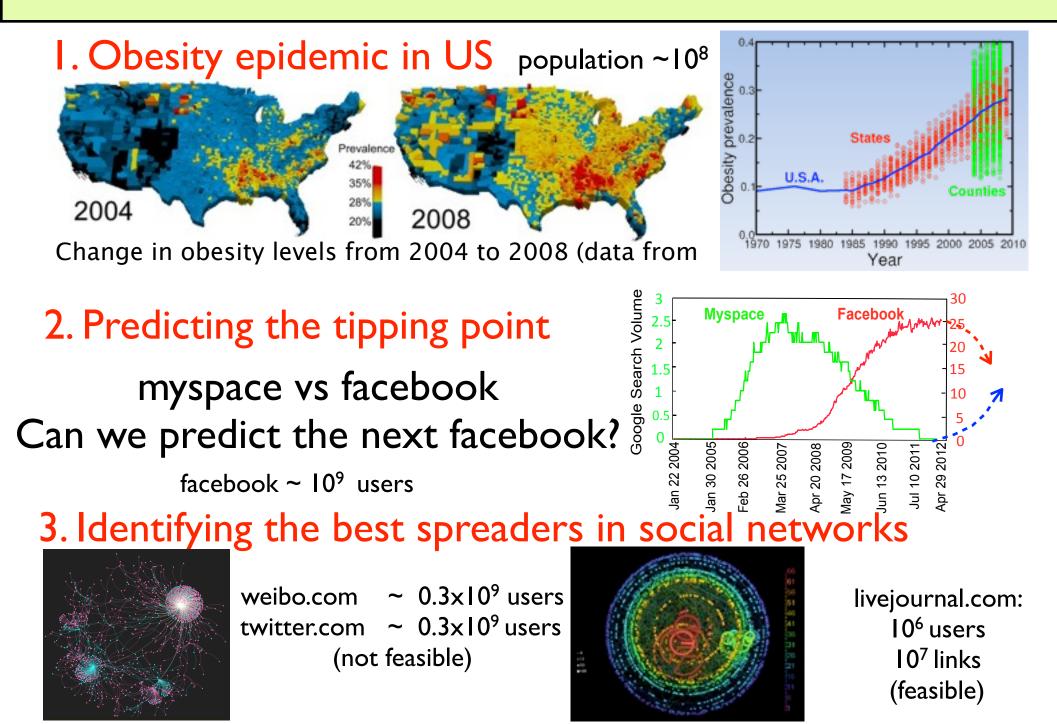


Conclusions

- Statistical physics applies to dissimilar problems involving big data: obesity epidemics and spreading of innovation.
- The percolation fragility model predicts the conditions for network fragmentation upon the departure of a few innovators.
- Tipping point happens when a network develops strong correlations between the hubs and the degree of influence.
- Results apply to any interconnected system with influence or dependency links, such as political networks, financial markets, infrastructure networks, power grids, etc.

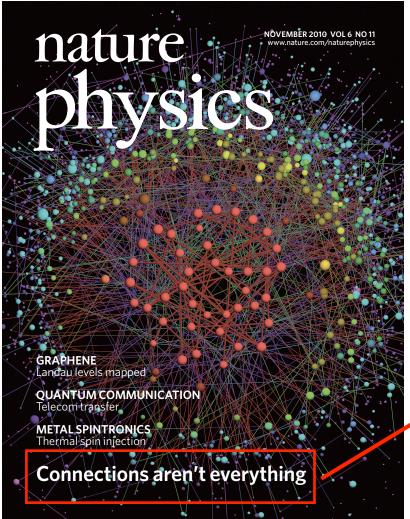


BIG DATA: Statistical physics: 10²³ molecules in a dm³ (Avogadro)



WHO ARE THE MOST INFLUENTIAL SPREADERS?

Who infects/influences the largest fraction of population?



Modeling disease spreading and spreading of information, rumors, etc

Applications:

1. Marketers: spreading of consumer products.

- 2. Vaccination strategies.
- 3. Break-up of a social network.

Location is more important: Who is at the center of the Web? Who is the central node in a social network?

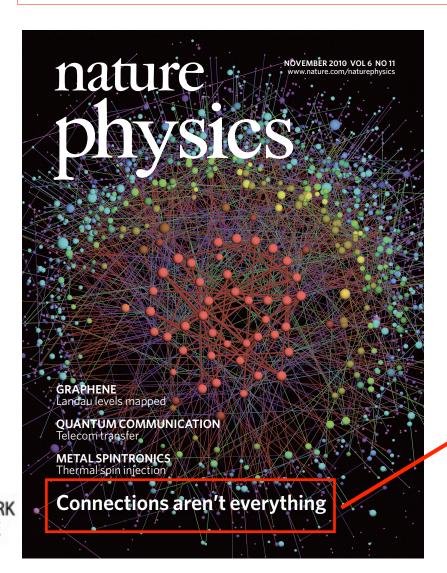




WHO ARE THE MOST INFLUENTIAL SPREADERS?



Not necessarily the most connected people!



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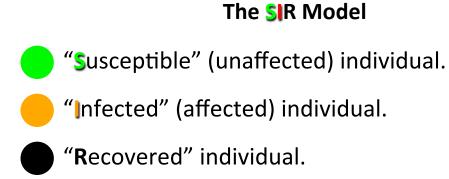
Location is more important: Who is at the center of the Web? Who is the central node in a social network?



Examples: Infectious diseases (smallpox, influenza, etc) Rumor, ideas Email, bluetooth viruses

Transmission rate $\beta = 0.5$ Recovery rate $\mu = 0.5$





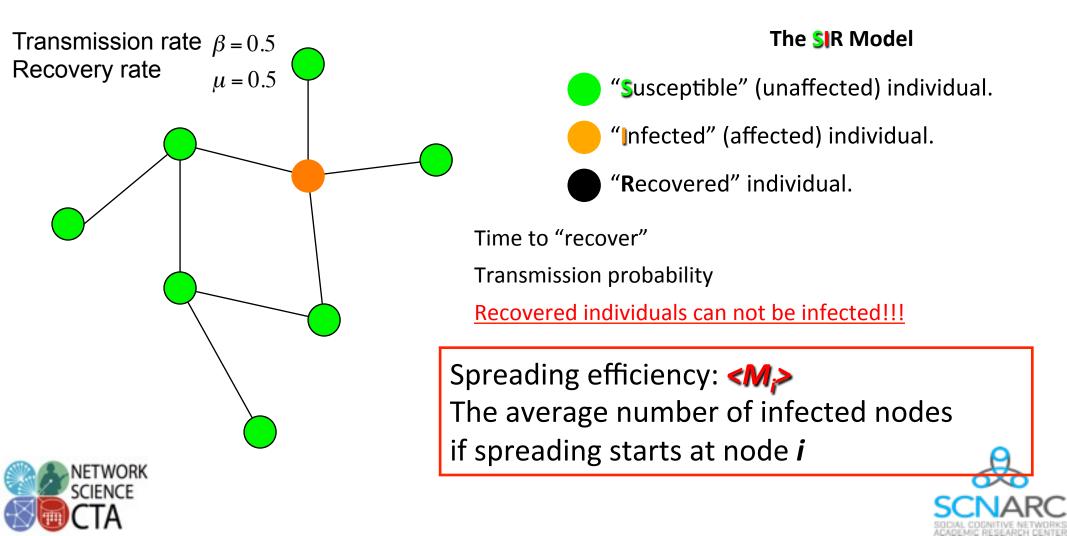
Time to "recover"

Transmission probability

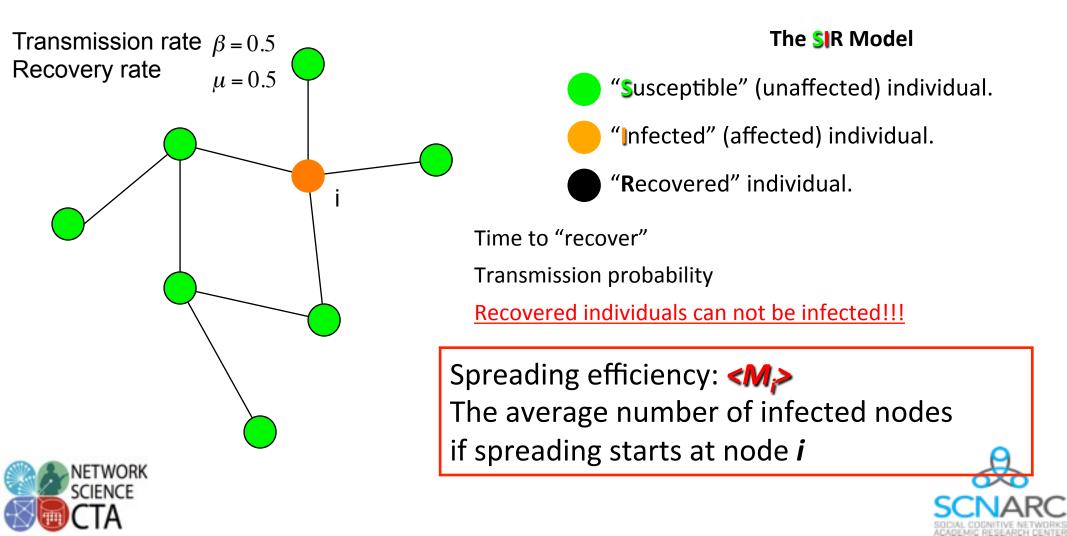
Recovered individuals can not be infected!!!

Spreading efficiency: <//>
Markow Spreading efficiency:
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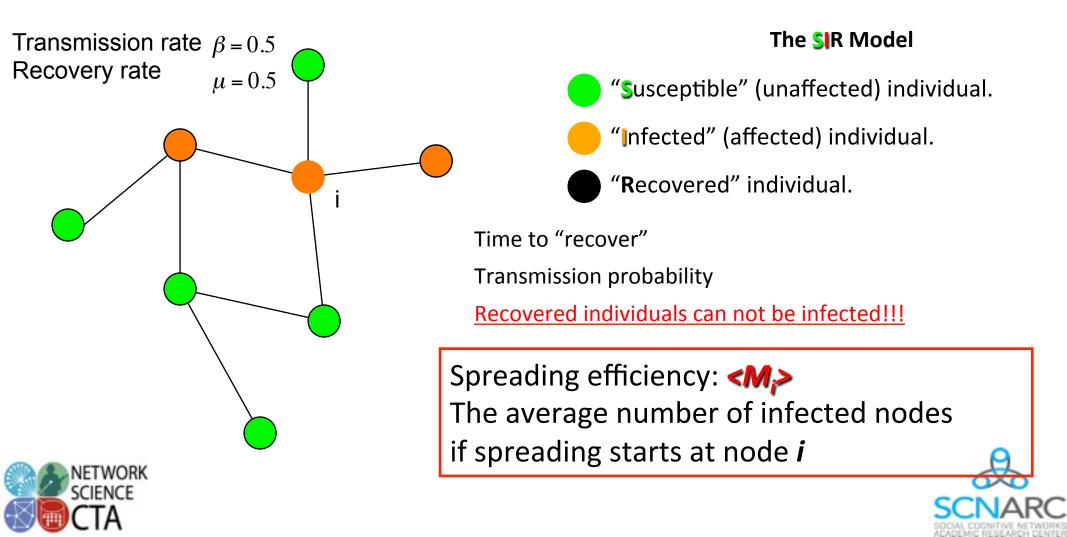




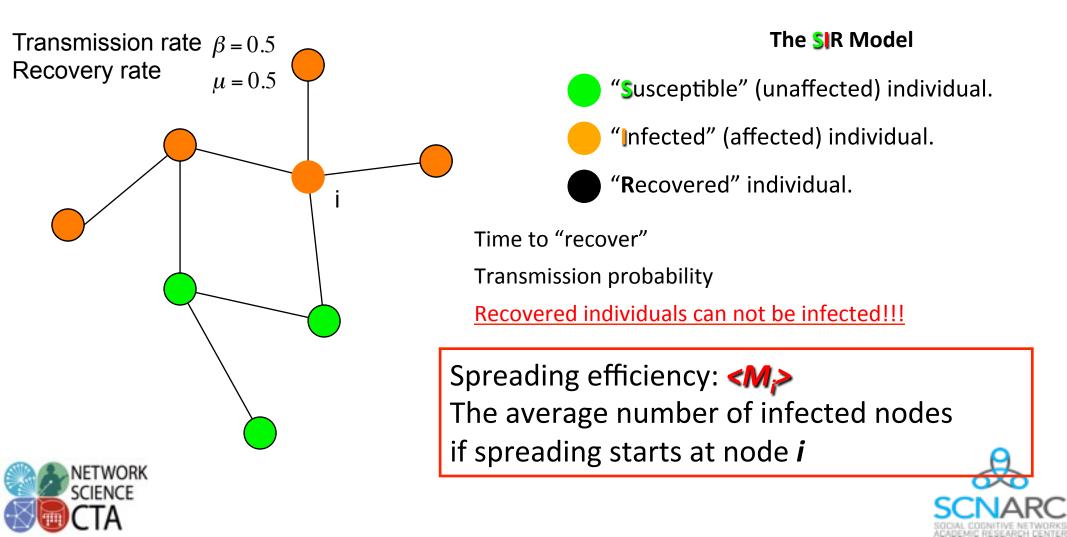




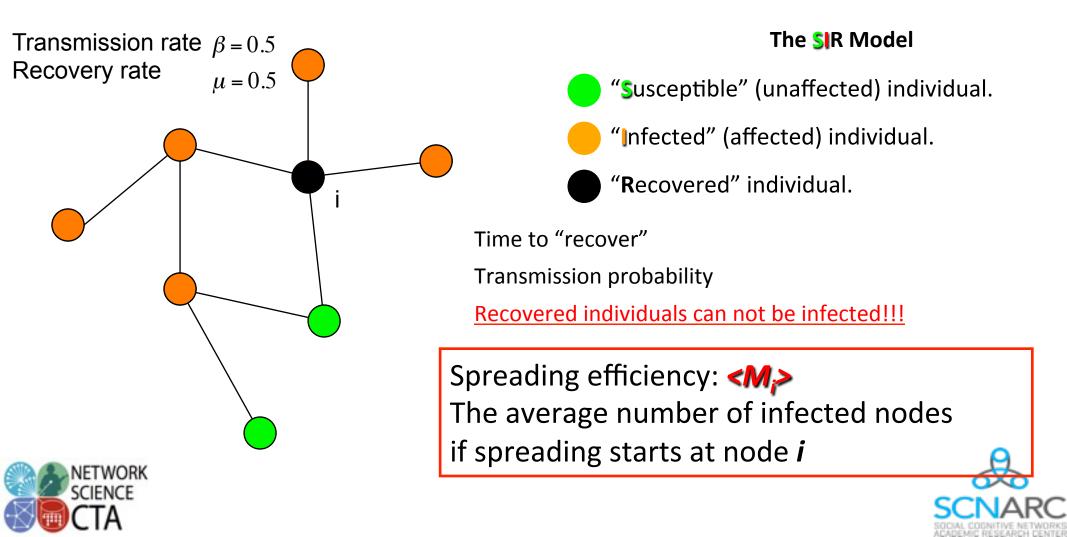




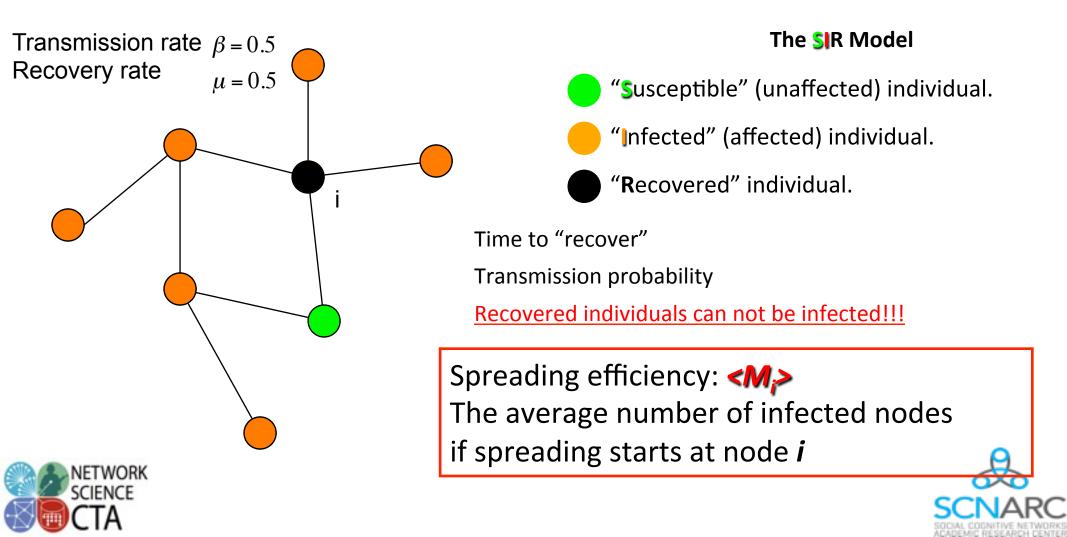




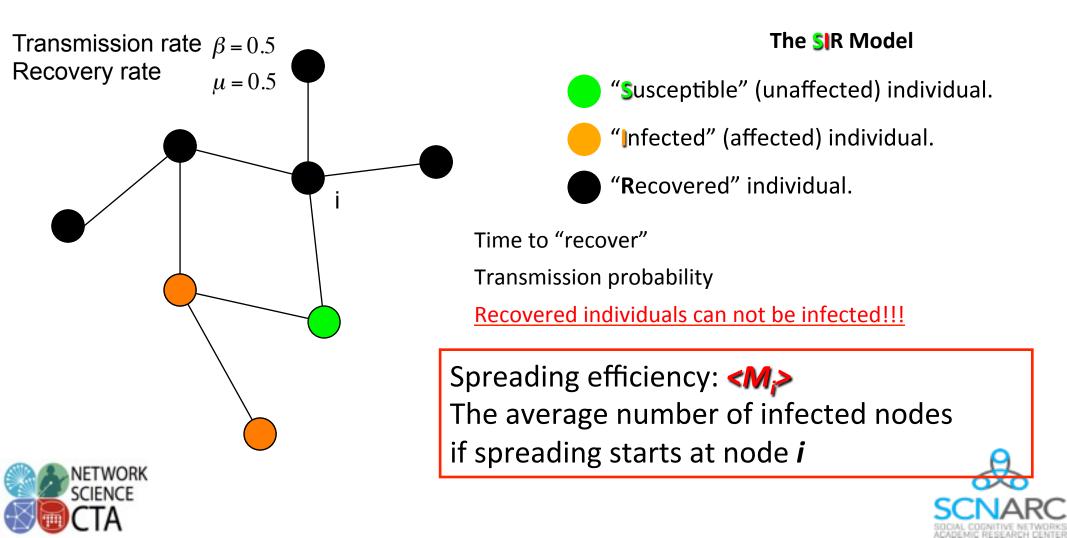




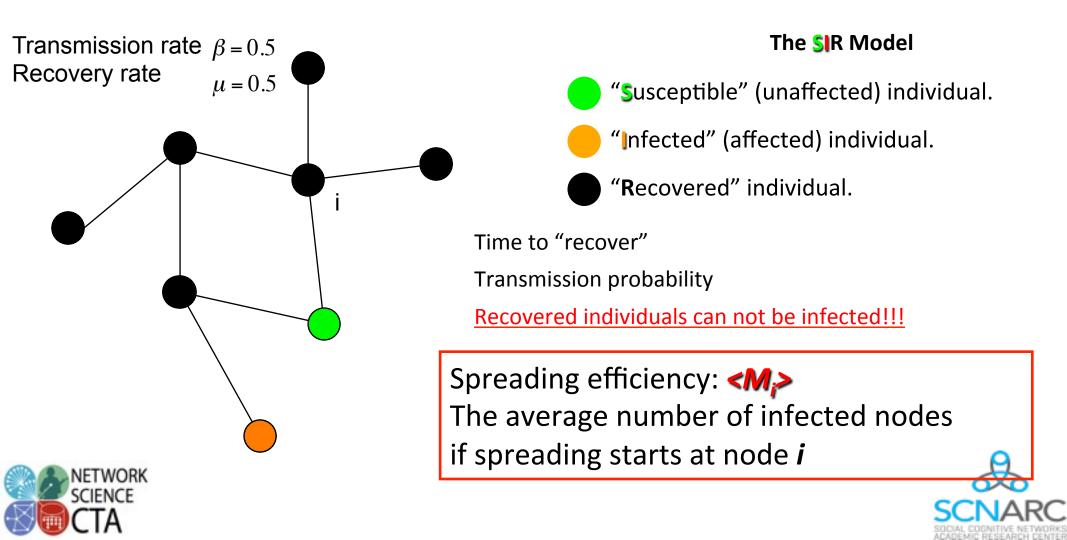








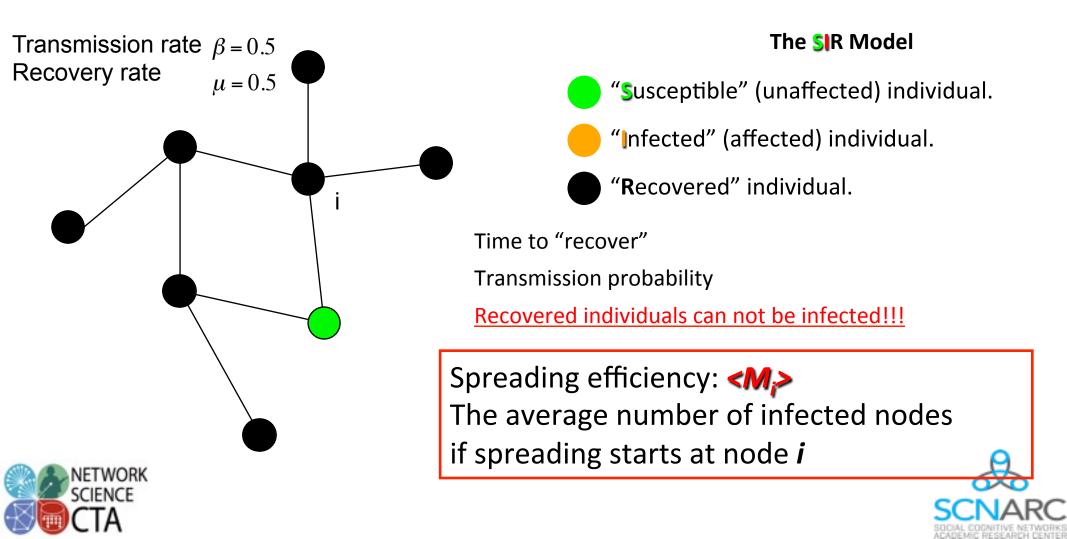




RDECOM Spreading process: models



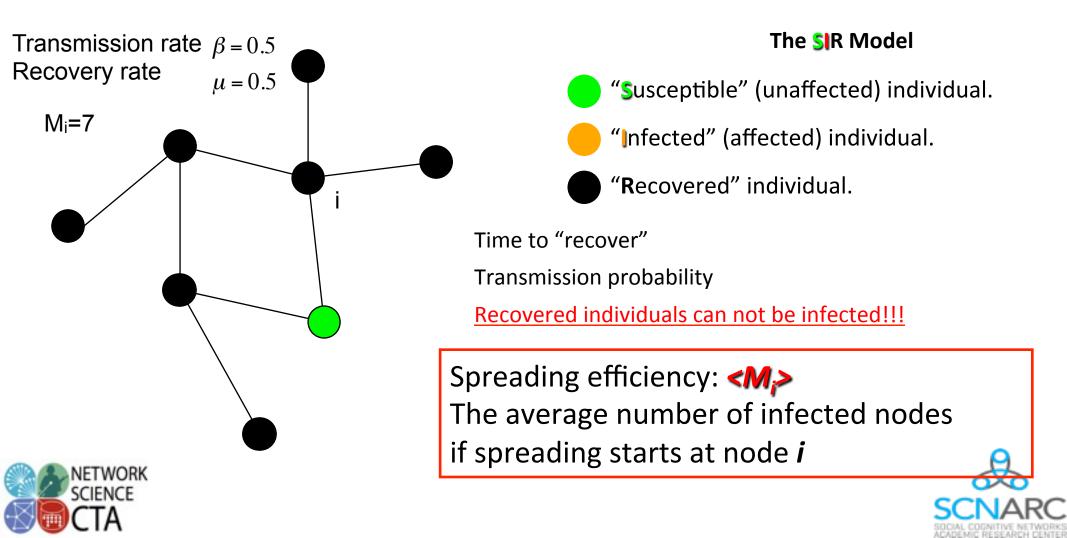
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RDECOM Spreading process: models

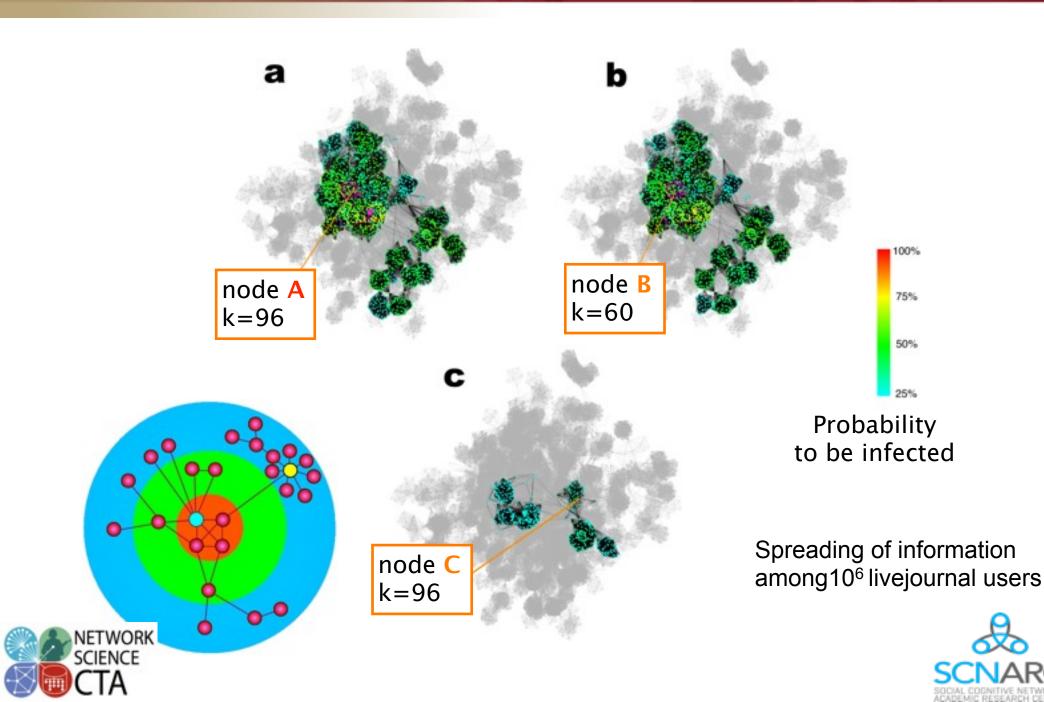


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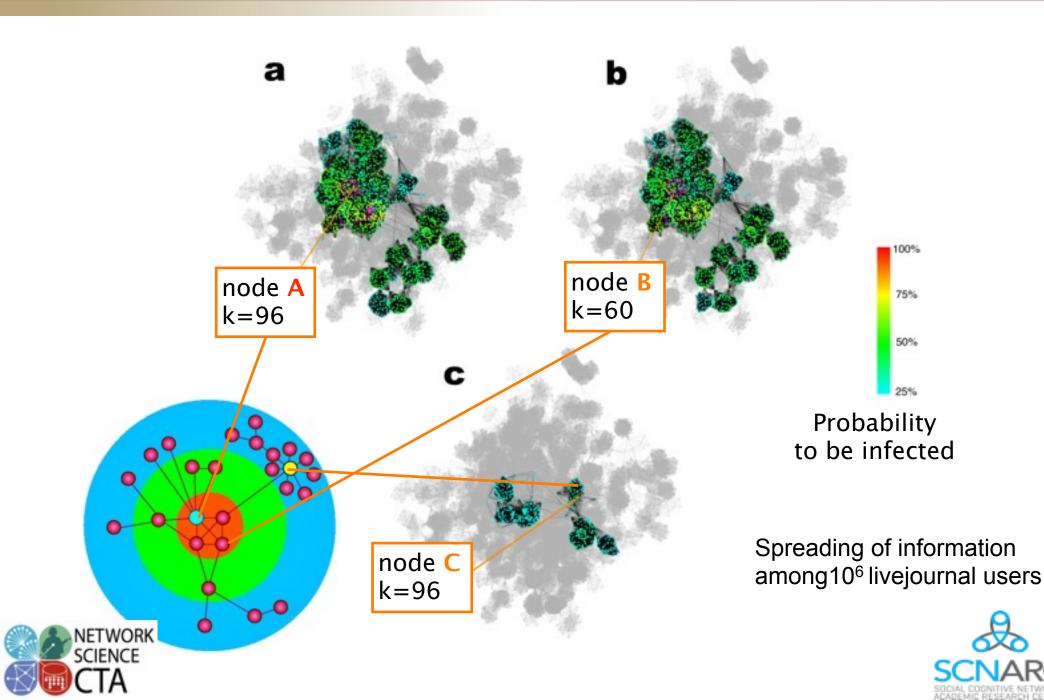
SPREADING EFFICIENCY IS DETERMINED BY LOCATION

RDECOM



SPREADING EFFICIENCY IS DETERMINED BY LOCATION

RDECOM



K-CORE DETERMINES NODE LOCATION (NODE VS PERIPHERY)

K-core: sub-graph with nodes of degree at least k inside the sub-graph.

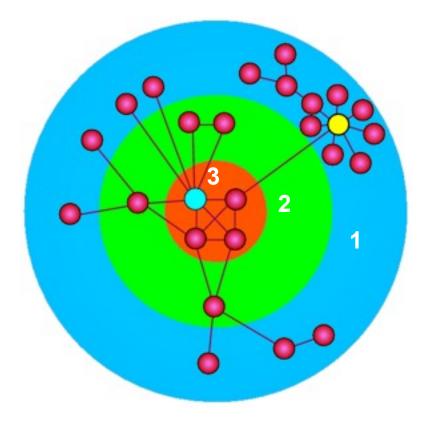
Pruning Rule:

1)Remove all nodes with k=1.

RNFCOM

Task S2.2

- Some remaining nodes may now have k = 1.
- 2) Repeat until there is no nodes with k = 1.
- 3) The remaining network forms the 2-core.
- 4) Repeat the process for higher k to extract other cores



K-shell is a set of nodes that belongs to the K-core

but NOT to the K+1-core

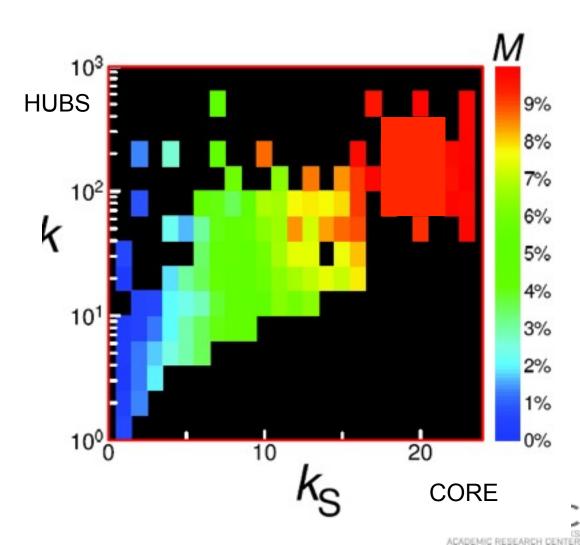






(1) For every individual *i* measure the average fraction of individuals M_i

- he or she would infect (spreading efficiency).
- (2) Group individuals based on the number of connections and the k-shell value.





RDECOM

Task S2.2

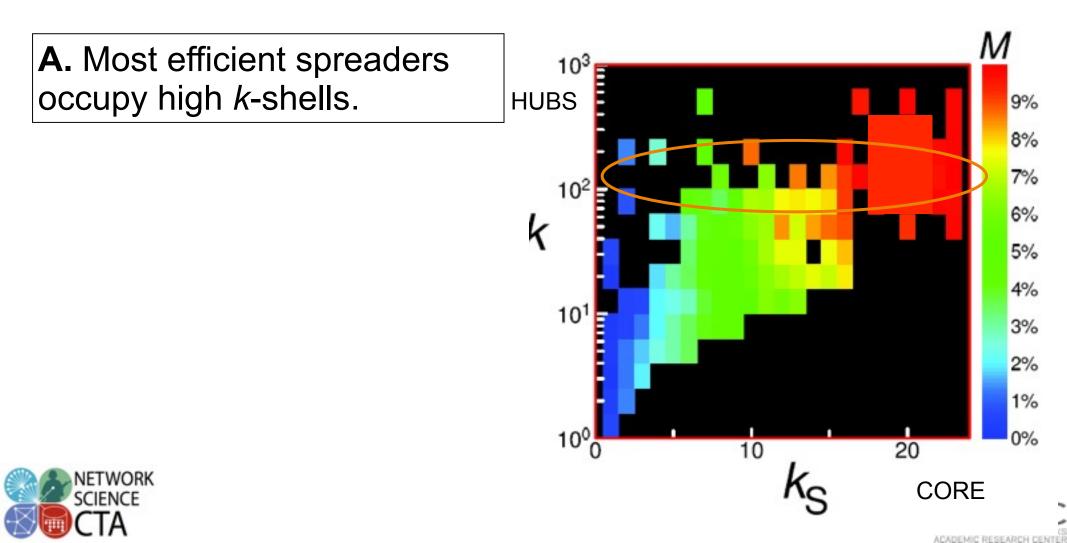




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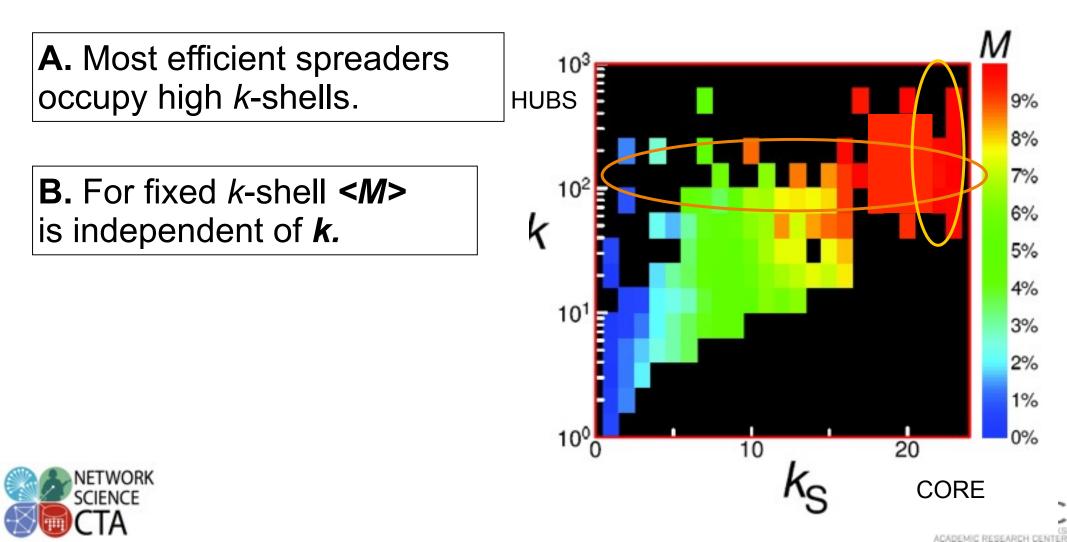




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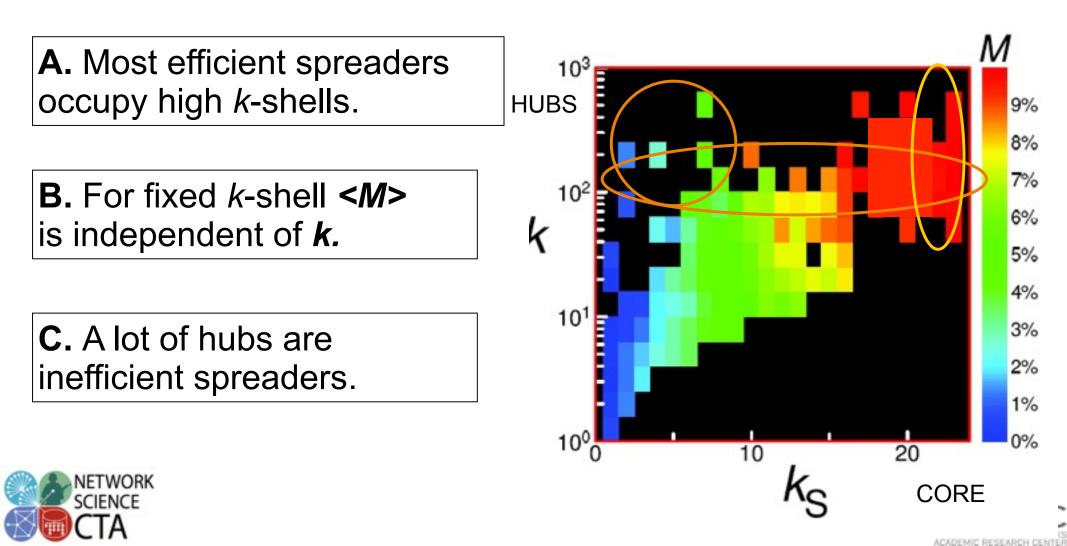




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Take home message









A. The most influential spreaders are not the hubs









A. The most influential spreaders are not the hubs

B. Most influential spreaders occupy the core of the networks as given by large k-shell









B. Most influential spreaders occupy the core of the networks as given by large k-shell

C. A lot of hubs are inefficient spreaders.





RDECOMS2.2 Forming, Dissolving, and InfluencingTask S2.2Communities in Social Networks

DRIVERS OF SOCIAL NETWORK FORMATION AND THE SPREADING OF IDEAS

Lazaros Gallos, Hernan A. Makse (PI)

Levich Institute and Physics Department City College of New York, CUNY

(Collaboration with RPI, NEU)

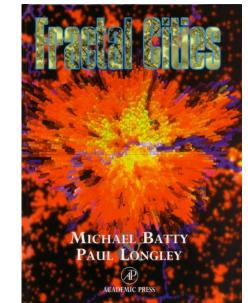




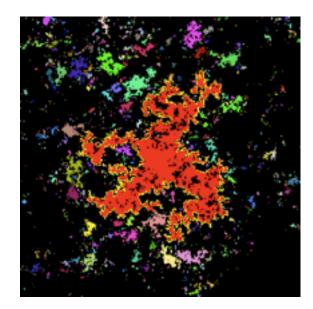
- I. Our analysis suggest that obesity spreading is similar to a critical point.
- 2. Long-range correlations are observed in many other indicators.
- 3.We classify the indicators in universality classes.4.The results suggest that a main driver for the
- obesity epidemic is the food marketing forces in detriment of individual habits.
- 5. This result might help in designing efficient health policies.

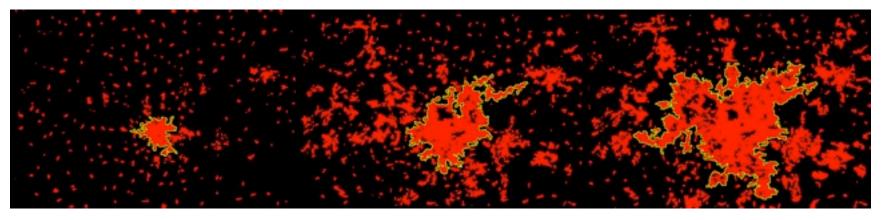
BIG DATA

DLA model: for Fractal Cities



Long-range percolation model of London





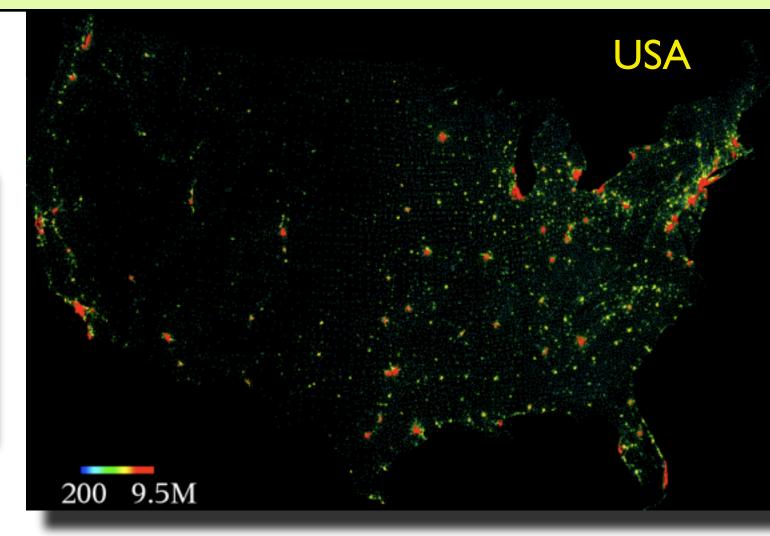
1875 1920 1945 Growth of Berlin

Next: City Clustering Algorithm (CCA)

How to define a city beyond admin boundaries.



London

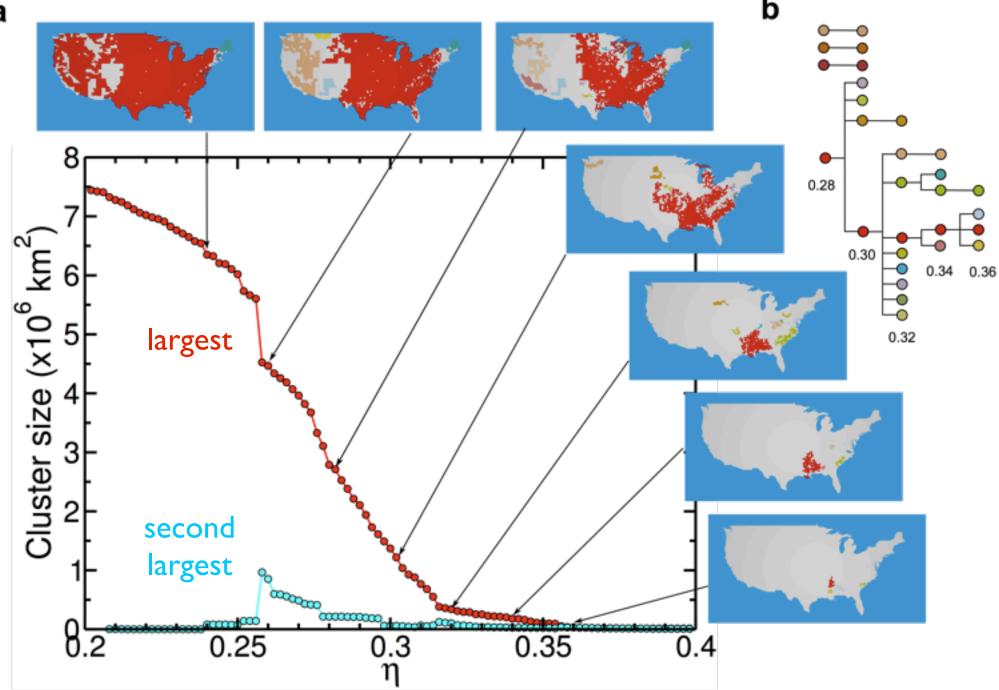


Gibrat Law fails: Rozenfeld, Andrade, Batty, Stanley, Makse. PNAS (2009) Zipf Law works: Rozenfeld, Gabaix, Makse. American Economic Review (2011)

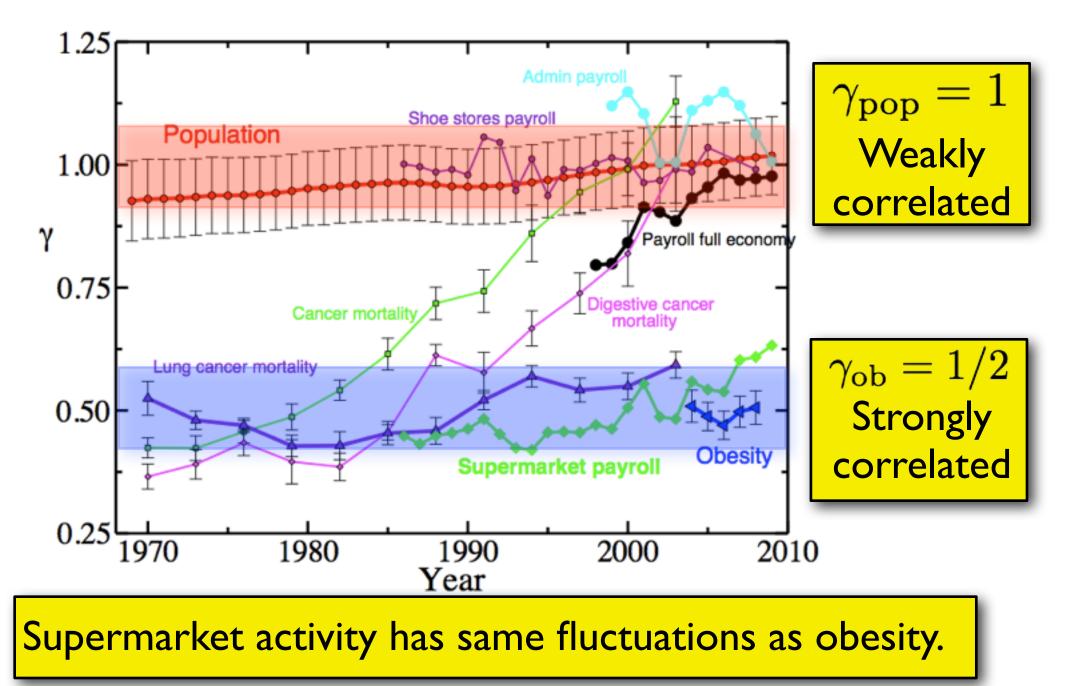
Work in progress: how to reconcile Zipf law without Gibrat

Hierarchical obesity percolation

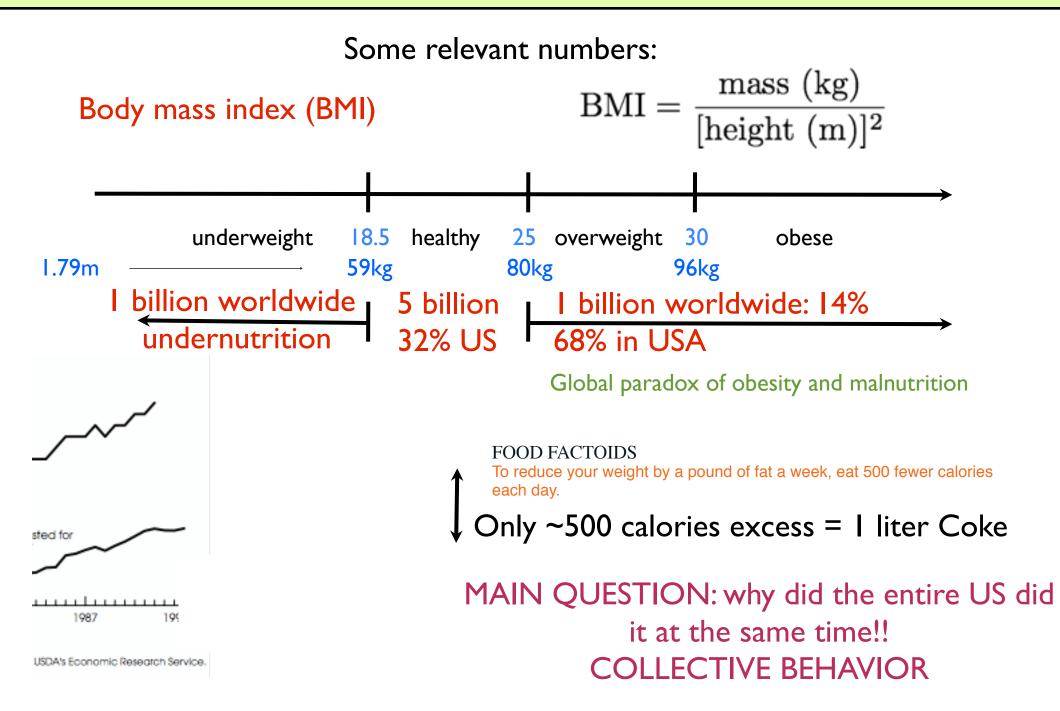
neither second order nor first order (Achlioptas)



Conclusion II: supermarket = obesity

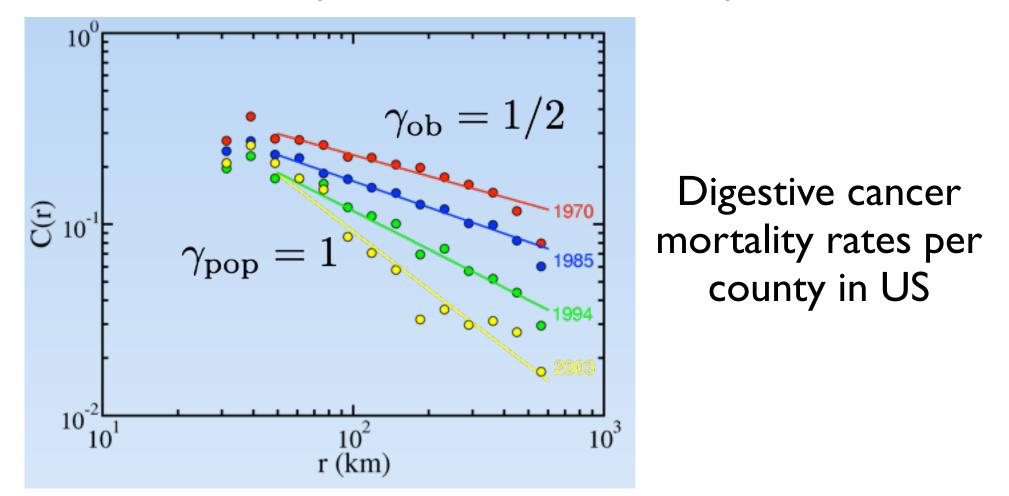


Alarming numbers! (not so..)



Test universality with other indicators

Test universality: Economic indicators, mortality rates, etc

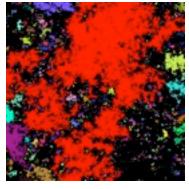


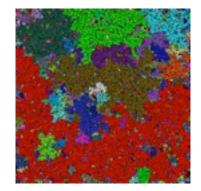
Dramatic change from strong correlations to weak correlations

Morphology of cities: a variation of percolation

Correlated gradient percolation model

Correlated clusters: development attracts more development. Preferential attachment Simon 1955 "rich gets richer"



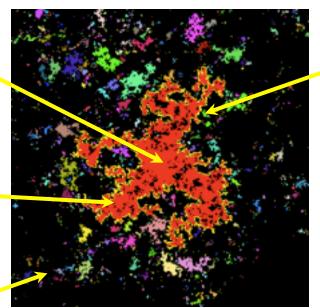


Uncorrelated percolation

Fractal model of London

Center above percolation

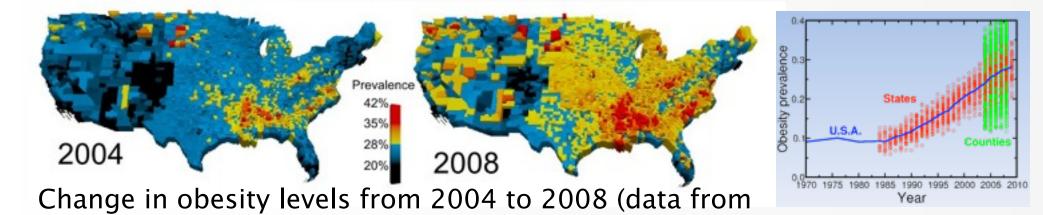
Gradient: Density of occupied sites decreases with distance

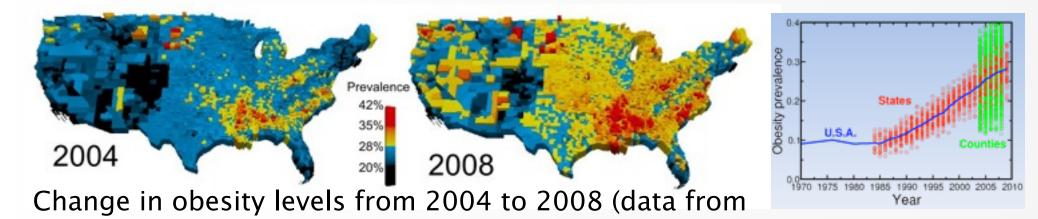


Urban Boundary is at critical percolation with fractal dimension

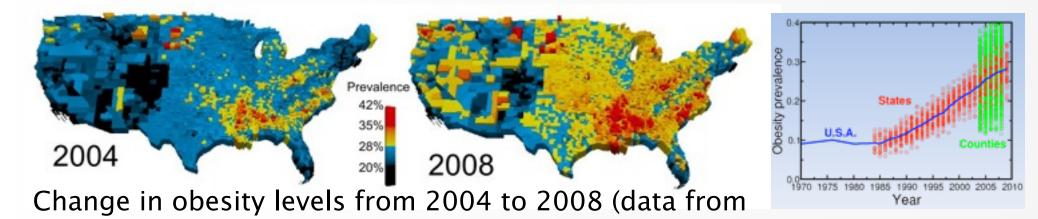
 $d_e \approx 1.3$

Satellite cities are below critical percolation



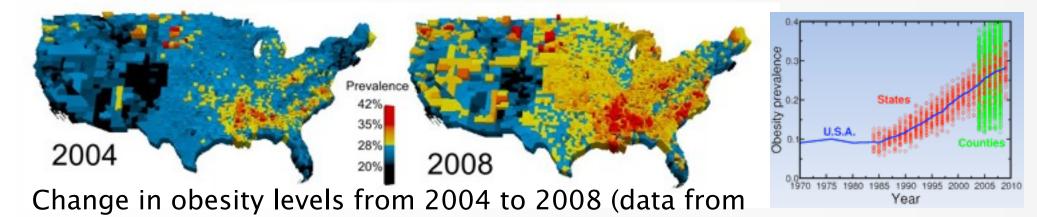


How to fight back: Recognize the drivers: Individual vs government/industry responsibility (hot debate!)



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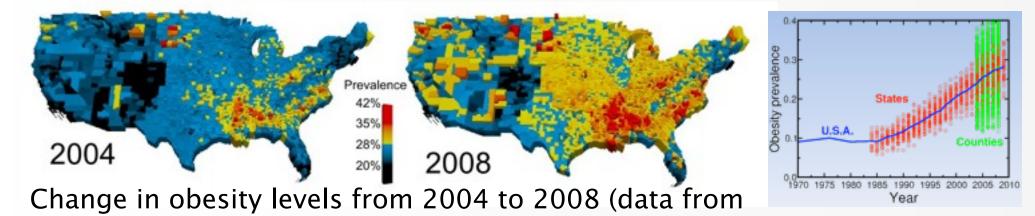
Our approach: Consider obesity rates in each county as the 'particles' of a physical system



How to fight back: Recognize the drivers: Individual vs government/industry responsibility (hot debate!)

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Methodology: Study how 'synchronized' is the obesity as we increase the counties distance (correlation)

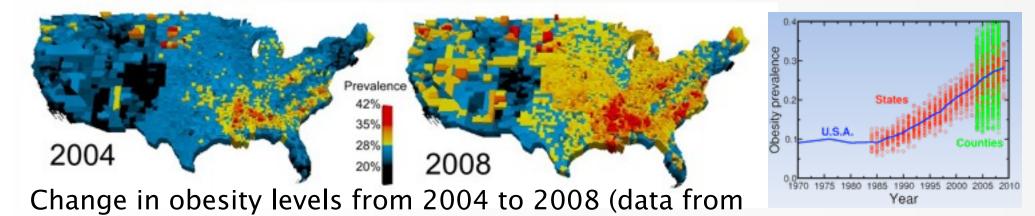


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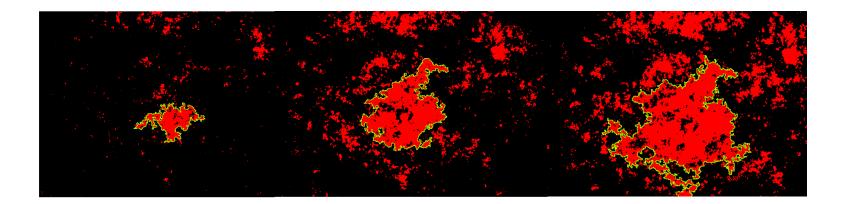
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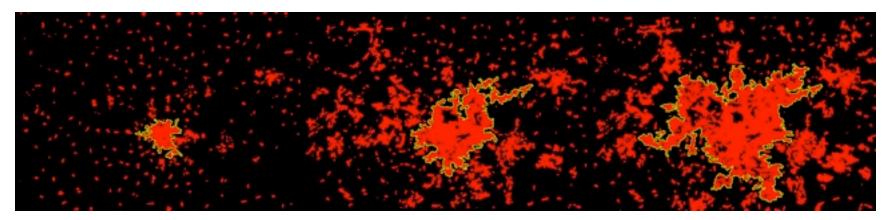
What this means: Individual behaviors are not important

Morphology of cities

Makse, Havlin, Stanley Nature (1995)

Growth of Correlated Percolation Model





1920 1945 Growth of Berlin

1875

Marion What are the drivers of the epidemic? Nestle, NYU



MAIN ISSUE: Individual responsability vs Industry/Goverment responsibility Social economic forces promoting calorie imbalance:

I. Overabundance of food: Role of supermarkets and marketing forces.
2. Exacerbated by deregulation of food industry in '80 (Reagan administration).
3. Blame Wall Street! Advent of the "shareholder value movement" in '80.

Demand for higher profit by food industry.

4. Obesity as a normal outcome of market economies.

5. Obesity as an "economic bubble".

See the movie: Foods Inc. www.foodincmovie.com

OUTLINE

Application of paradigms of equilibrium statistical physics to help explain a different set of natural phenomena.

Systems:

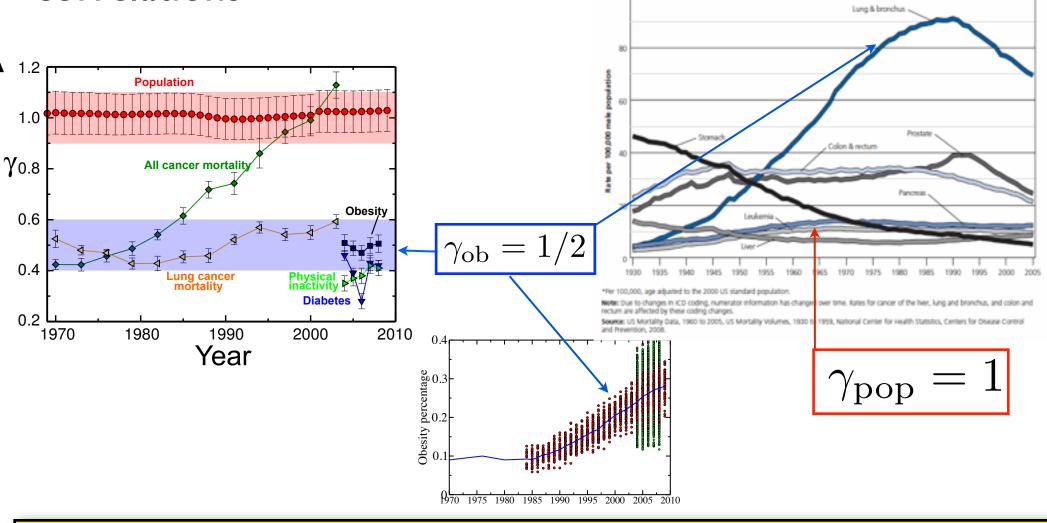
I. Obesity epidemic: geographical clustering and drivers
2. Rise and fall of social communities: cascades of followers triggered by pioneers

Commonality: Clustering and correlations in human activity.

Tools: Percolation theory and collective behavior in complex systems.

Conjecture 2

A close relation between rapid growth and strong correlations



Are all exponentially growing activities in $\gamma_{
m ob} = 1/2$?